

# 通过 $T_{cc}$ 的研究得到 $D\bar{D}^*$ 耦合系统的 物理图像

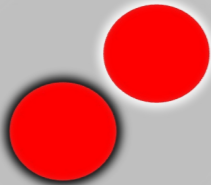
杨智

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Based on [Sci.Bull. 69,3036\(2024\)](#)

In collaboration with 王广娟, 吴佳俊, Makoto Oka, 朱世琳

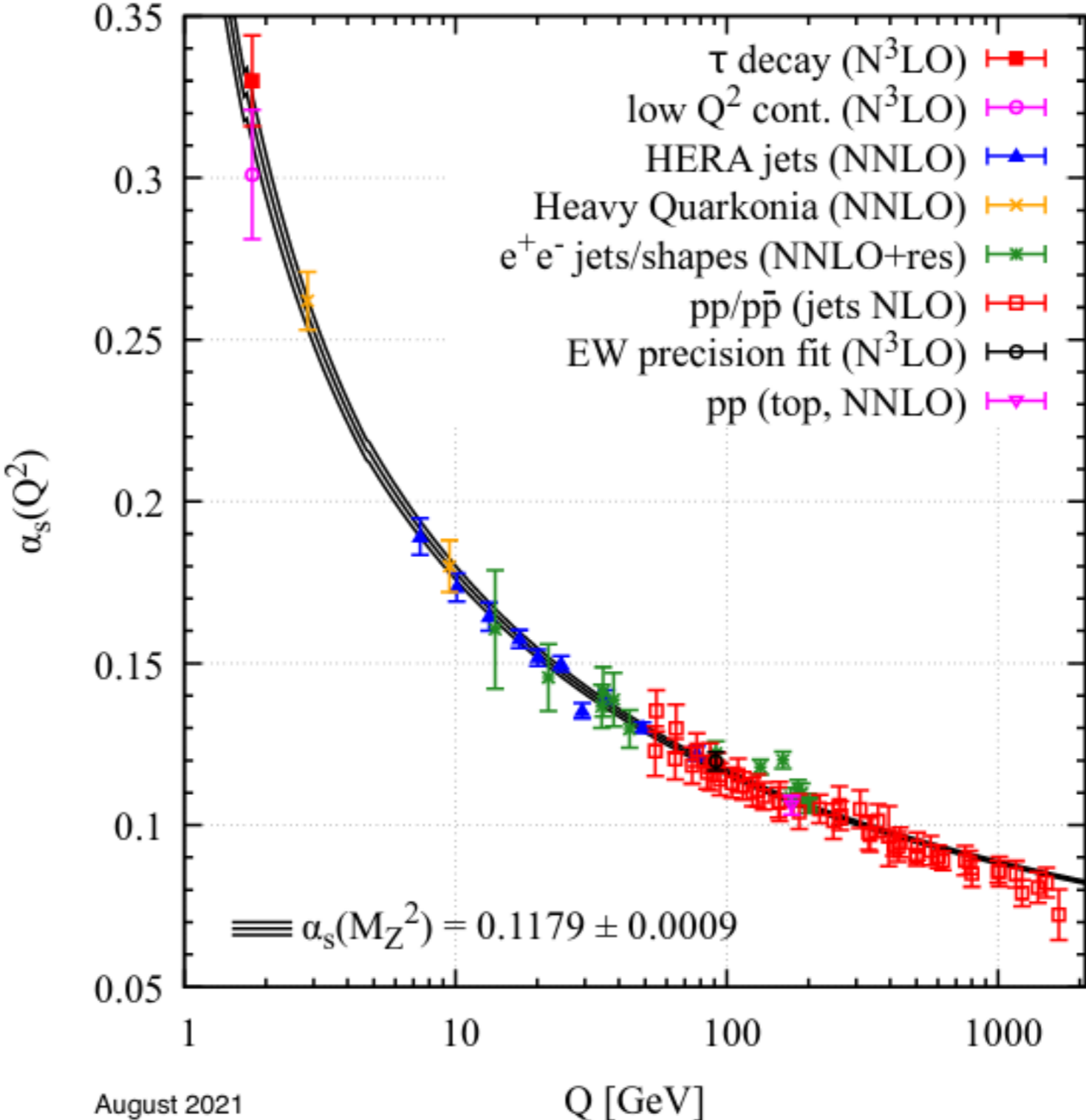
非微扰方法及其在高能物理中的应用专题研讨会, 中国科学技术大学, 2024/10/24



Meson



Baryon



August 2021

The running coupling constant

## A SCHEMATIC MODEL OF BARYONS AND MESONS \*

M. GELL-MANN

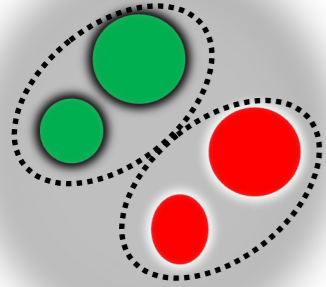
California Institute of Technology, Pasadena, California

Received 4 January 1964

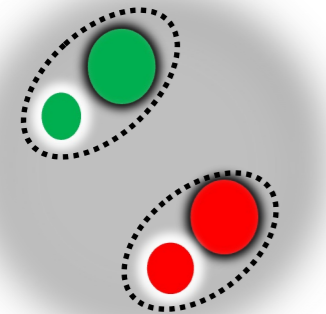
If we assume that the strong interactions of baryons and mesons are correctly described in terms of the broken "eightfold way" <sup>1-3</sup>, we are tempted to look for some fundamental explanation of the situation. A highly promised approach is the purely dynamical "bootstrap" model for all the strongly interacting particles within which one may try to derive isotopic spin and strangeness conservation and broken eightfold symmetry from self-consistency alone <sup>4</sup>. Of course, with only strong interactions, the orientation of the asymmetry in the unitary space cannot be specified; one hopes that in some way the selection of specific components of the F-spin by electromagnetism and the weak interactions determines the choice of isotopic spin and hypercharge directions.

ber  $n_t - n_{\bar{t}}$  would be zero for all known baryons and mesons. The most interesting example of such a model is one in which the triplet has spin  $\frac{1}{2}$  and  $z = -1$ , so that the four particles  $d^-$ ,  $s^-$ ,  $u^0$  and  $b^0$  exhibit a parallel with the leptons.

A simpler and more elegant scheme can be constructed if we allow non-integral values for the charges. We can dispense entirely with the basic baryon  $b$  if we assign to the triplet  $t$  the following properties: spin  $\frac{1}{2}$ ,  $z = -\frac{1}{3}$ , and baryon number  $\frac{1}{3}$ . We then refer to the members  $u^{\frac{2}{3}}$ ,  $d^{-\frac{1}{3}}$ , and  $s^{-\frac{1}{3}}$  of the triplet as "quarks" <sup>6)</sup>  $q$  and the members of the anti-triplet as anti-quarks  $\bar{q}$ . Baryons can now be constructed from quarks by using the combinations  $(qqq)$ ,  $(qqq\bar{q}\bar{q})$ , etc., while mesons are made out of  $(q\bar{q})$ ,  $(qq\bar{q}\bar{q})$ , etc. It is assuming that the lowest



Compact multiquark



Hadronic molecule

8419/TH.412  
21 February 1964

AN  $SU_3$  MODEL FOR STRONG INTERACTION SYMMETRY AND ITS BREAKING

II \*)

G. Zweig

CERN---Geneva

\*) Version I is CERN preprint 8182/TH.401, Jan. 17, 1964.

...

6) In general, we would expect that baryons are built not only from the product of three aces,  $AAA$ , but also from  $\bar{A}AAAA$ ,  $\bar{A}AAAAA$ , etc., where  $\bar{A}$  denotes an anti-ace. Similarly, mesons could be formed from  $\bar{A}A$ ,  $\bar{A}AAA$  etc. For the low mass mesons and baryons we will assume the simplest possibilities,  $\bar{A}A$  and  $AAA$ , that is, "deuces and treys".



## The relativized quark model:

$$H = H_0 + V$$

$$H_0 = \sqrt{m_1^2 + p^2} + \sqrt{m_2^2 + p^2}$$

$$V = G_{\text{eff}}(r) + S_{\text{eff}}(r)$$

$$H|\psi_\alpha\rangle = M_\alpha^0|\psi_\alpha\rangle \longrightarrow \text{Mass \& wave function}$$

### Mesons in a Relativized Quark Model with Chromodynamics

#1

S. Godfrey (Toronto U.), Nathan Isgur (Toronto U.) (1985)

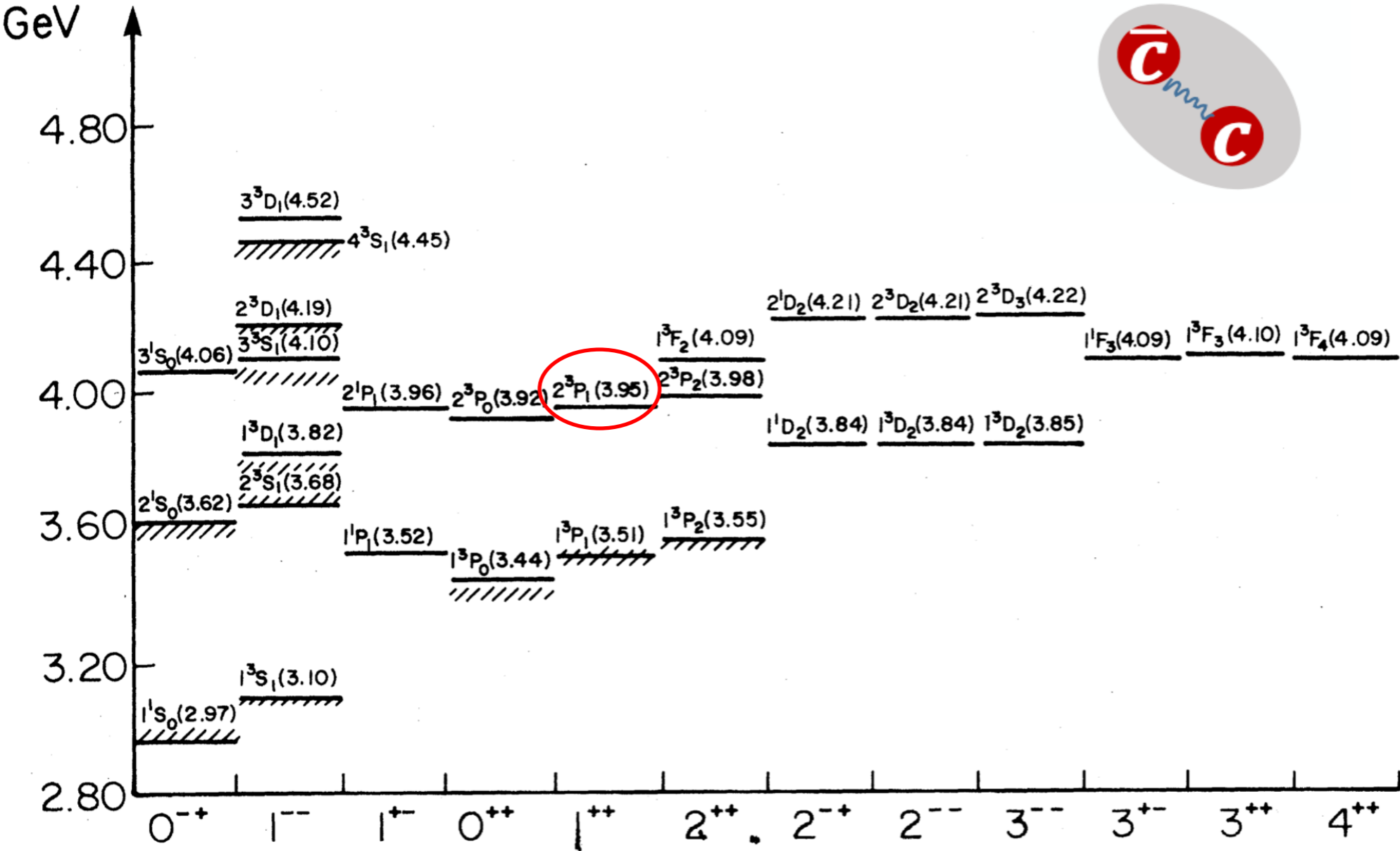
Published in: *Phys.Rev.D* 32 (1985) 189-231

[DOI](#) [cite](#) [claim](#)

[reference search](#)

[3,134 citations](#)

# Charmonium state in the GI quark model



Godfrey, Isgur, PRD32,189



Experiment	Mass [MeV]	Width [MeV]
Belle [63]	$3872 \pm 0.6 \pm 0.5$	$< 2.3$
Belle [75]	–	–
Belle [76]	$3875.4 \pm 0.7^{+0.4}_{-1.7} \pm 0.9$	–
Belle [77]	$3871.46 \pm 0.37 \pm 0.07$	–
Belle [78]	$3872.9^{+0.6+0.4}_{-0.4-0.5}$	$3.9^{+2.8+0.2}_{-1.4-1.1}$
Belle [79]	–	–
Belle [80]	$3871.84 \pm 0.27 \pm 0.19$	$< 1.2$
CDF [67]	$3871.3 \pm 0.7 \pm 0.4$	–
CDF [81]	–	–
CDF [82]	–	–
CDF [83]	$3871.61 \pm 0.16 \pm 0.19$	–
DØ [68]	$3871.8 \pm 3.1 \pm 3.0$	–
BaBar [84]	$3873.4 \pm 1.4$	–
BaBar [85]	$3871.3 \pm 0.6 \pm 0.1$	$< 4.1$
	$3868.6 \pm 1.2 \pm 0.2$	–
BaBar [86]	–	–
BaBar [87]	$3875.1^{+0.7}_{-0.5} \pm 0.5$	$3.0^{+1.9}_{-1.4} \pm 0.9$
BaBar [88]	$3871.4 \pm 0.6 \pm 0.1$	$< 3.3$
	$3868.7 \pm 1.5 \pm 0.4$	–
BaBar [89]	–	–
BaBar [90]	$3873.0^{+1.8}_{-1.6} \pm 1.3$	–
LHCb [91]	$3871.95 \pm 0.48 \pm 0.12$	–
LHCb [70]	–	–
LHCb [92]	–	–
CMS [73]	–	–
BESIII [93]	$3871.9 \pm 0.7 \pm 0.2$	$< 2.4$

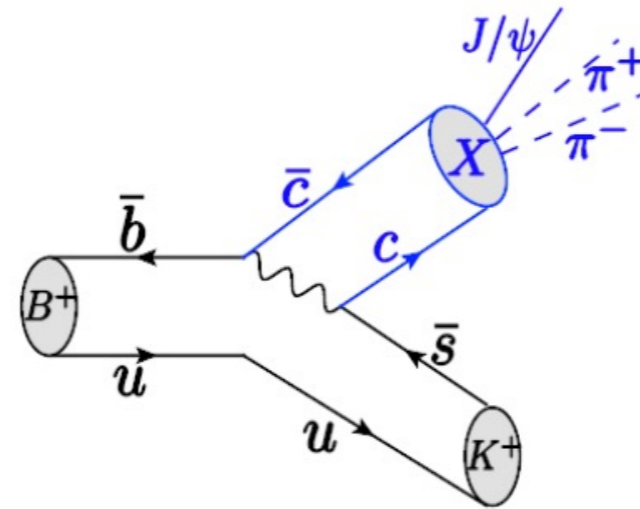
## Observation of a narrow charmonium-like state in exclusive $B^\pm \rightarrow K^\pm \pi^+ \pi^- J/\psi$ decays

Belle Collaboration • S.K. Choi (Gyeongsang Natl. U.) et al. (Sep, 2003)

Published in: *Phys.Rev.Lett.* 91 (2003) 262001 • e-Print: [hep-ex/0309032](https://arxiv.org/abs/hep-ex/0309032) [hep-ex]

[pdf](#) [links](#) [DOI](#) [cite](#) [claim](#)

2,295 citations

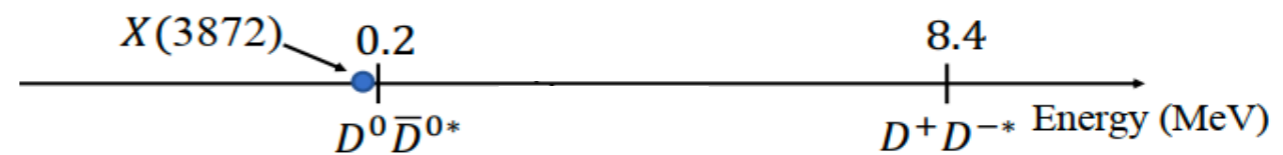


Close to  $D^0 \bar{D}^{*0} / D^{*0} \bar{D}^0$  thresholds

$$\delta m = m_{D^0 \bar{D}^{*0}} - m_{X(3872)}$$

$$= 0.00 \pm 0.18 \text{ MeV}$$

PDG 22



- The  $D\bar{D}^*/D^*\bar{D}$  molecular state.

Swanson, Wong, Guo, Liu,....

## Where is the $\chi_{c1}(2P)$ in quark model?

- The mixing of the  $\bar{c}c$  core with  $D\bar{D}^*/D^*\bar{D}$  component.

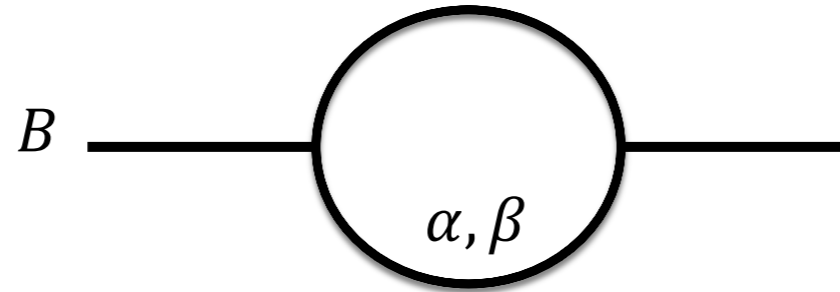
Chao, H. Q. Zheng, Yu. S. Kalashnikova, P. G. Ortega...

Close to charmonium  $\chi_{c1}(2P)$ :  $m=3953.5$  MeV

$$\delta m = m_{\chi_{c1}(2P)} - m_{X(3872)} = 81.35 \text{ MeV}$$

→ *Complicated coupled-channel effect:  $\bar{c}c$  &  $D\bar{D}^*/D^*\bar{D}$*

Phys. Rev. D 32, 189 (1985)

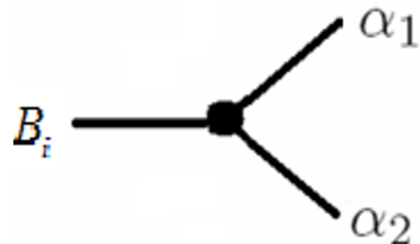


- Coupled-channel effect due to hadron loop could cause sizable mass shift on the state in quark model.
- In the T-matrix, the

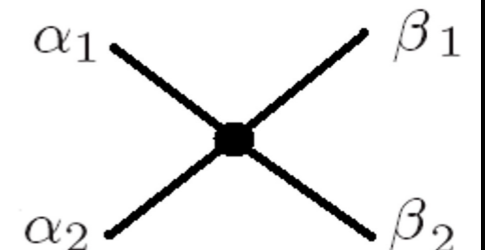
$$T(\vec{k}_{D^*}, \vec{k}'_{D^*}; E) = \mathcal{V}(\vec{k}_{D^*}, \vec{k}'_{D^*}; E) + \int d\vec{q} \frac{\mathcal{V}(\vec{k}_{D^*}, \vec{q}; E) T(\vec{q}, \vec{k}'_{D^*}; E)}{E - \sqrt{m_D^2 + q^2} - \sqrt{m_{D^*}^2 + q^2} + i\epsilon}$$

$$\mathcal{V}(\vec{k}_{D^*}, \vec{k}'_{D^*}; E) = \frac{g(\vec{k}_{D^*})g(\vec{k}'_{D^*})}{E - m_B} + v(\vec{k}_{D^*}, \vec{k}'_{D^*})$$

bare state core  $\rightarrow$  channel:

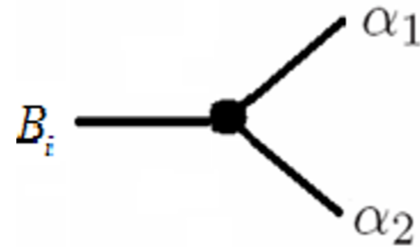


channel  $\rightarrow$  channel:

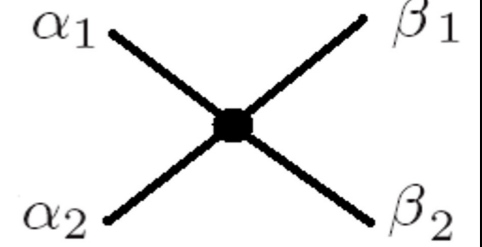




bare state core  $\rightarrow$  channel:



channel  $\rightarrow$  channel:



Z. Yang, G.J. Wang, J.J. Wu, M. Oka, S.L. Zhu, Phys.Rev.Lett. 128,112001(2022)

$$g = \sum_{\alpha, B} \int d^3 \vec{k} \left\{ |\alpha(\vec{k})\rangle g_{\alpha B}(|\vec{k}|) \langle B| + h.c. \right\}$$

Quark pair creation model (QPC):

$$g_{\alpha B}(|\vec{k}|) = \gamma I_{\alpha B}(|\vec{k}|) e^{-\frac{\vec{k}^2}{2\Lambda'^2}}$$

P. G. Ortega, et al,  
Phys. Rev. D 94, 074037 (2016)

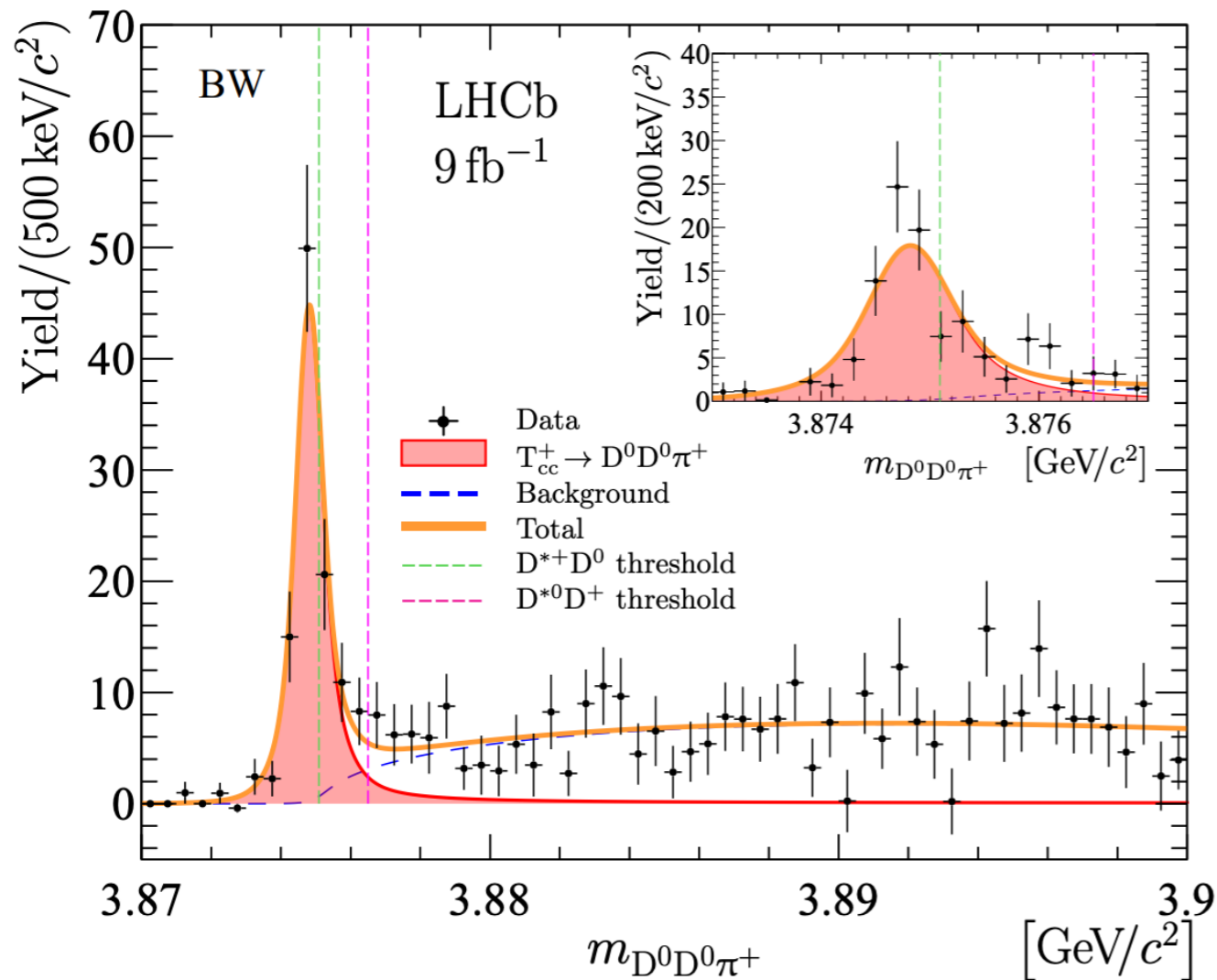
truncate the hard vertices  
given by usual QPC

$$v = \sum_{\alpha, \beta} \int d^3 \vec{k} d^3 \vec{k}' |\alpha(\vec{k})\rangle V_{\alpha, \beta}^L(|\vec{k}|, |\vec{k}'|) \langle \beta(\vec{k}')|$$

Effective Lagrangian: (exchanging  $\rho/\omega$ )

$$\begin{aligned} \mathcal{L} &= \mathcal{L}_{PPV} + \mathcal{L}_{VVV} \\ &= ig_v \text{Tr}(\partial^\mu P [P, V_\mu]) + ig_v \text{Tr}(\partial^\mu V^\nu [V_\mu, V_\nu]) \end{aligned}$$

# How to determine the component in the X(3872): from $T_{cc}$



- $D^0D^0\pi^+$  channel
- Close to  $D^{*+}D^0$  thresholds:

Conventional Breit-Wigner: assumed  $J^P = 1^+$ .

$$\begin{aligned} \delta m_{BW} &= m_{T_{cc}} - m_{D^{*+}D^0} \\ &= -273 \pm 61 \text{ keV} \end{aligned}$$

$$\Gamma_{BW} = 410 \pm 165 \text{ keV}$$

EPS-HEP conference, Ivan Polyakov's talk, 29/07/2021; Nature Physics, 22'

Unitarized Breit-Wigner:

$$\begin{aligned} \delta m_U &= m_{T_{cc}} - m_{D^{*+}D^0} \\ &= -361 \pm 40 \text{ keV} \end{aligned}$$

$$\Gamma_U = 47.8 \pm 1.9 \text{ keV}$$

LHCb, Nature Commun. 13 (2022) 1, 3351

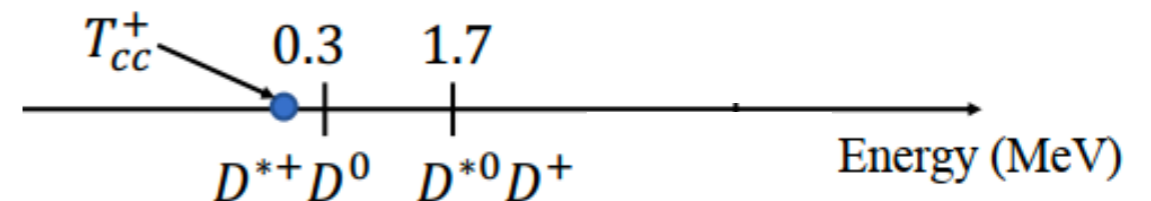
❖ Quark content:  $cc\bar{u}\bar{d}$

❖ *Only the  $D^*D$  coupled channel effect*



**C-parity**

$\bar{D}^*D / \bar{D}D^*$  interaction



$DD^*$

$$H_a^{(Q)} = \frac{1+\not{\epsilon}}{2} [P_a^{*\mu} \gamma_\mu - P_a \gamma_5]$$

$$\bar{H}_a^{(Q)} \equiv \gamma_0 H_a^{(Q)\dagger} \gamma_0 = [P_a^{*\dagger\mu} \gamma_\mu + P_a^\dagger \gamma_5] \frac{1+\not{\epsilon}}{2}$$

$$P = (D^0, D^+, D_s^+) \ \& \ P^* = (D^{*0}, D^{*+}, D_s^{*+})$$

$$\mathcal{L}_{MH^{(Q)}H^{(Q)}} = ig \text{Tr} \left[ H_b^{(Q)} \gamma_\mu \gamma_5 A_{ba}^\mu \bar{H}_a^{(Q)} \right]$$

$$\mathcal{L}_{VH^{(Q)}H^{(Q)}} = i\beta \text{Tr} \left[ H_b^{(Q)} v_\mu (V_{ba}^\mu - \rho_{ba}^\mu) \bar{H}_a^{(Q)} \right] \\ + i\lambda \text{Tr} \left[ H_b^{(Q)} \sigma_{\mu\nu} F^{\mu\nu}(\rho)_{ba} \bar{H}_a^{(Q)} \right]$$

$D\bar{D}^*$

$$H_a^{(\bar{Q})} \equiv C \left( C H_a^{(Q)} C^{-1} \right)^T C^{-1} = [P_{a\mu}^{(\bar{Q})*} \gamma^\mu - P_a^{(\bar{Q})} \gamma_5] \frac{1-\not{\epsilon}}{2}$$

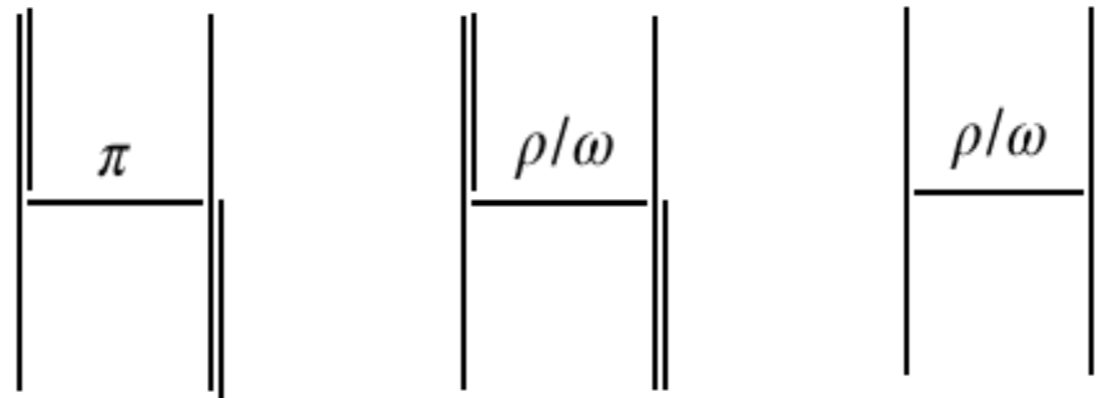
$$\bar{H}_a^{(\bar{Q})} \equiv \gamma_0 H_a^{(\bar{Q})\dagger} \gamma_0 = \frac{1-\not{\epsilon}}{2} [P_{a\mu}^{(\bar{Q})*\dagger} \gamma^\mu + P_a^{(\bar{Q})\dagger} \gamma_5]$$

$$\tilde{P} = (\bar{D}^0, D^-, D_s^-) \ \& \ \tilde{P}^* = (\bar{D}^{*0}, D^{*-}, D_s^{*-})$$

$$\mathcal{L}_{MH^{(\bar{Q})}H^{(\bar{Q})}} = ig \text{Tr} \left[ \bar{H}_a^{(\bar{Q})} \gamma_\mu \gamma_5 A_{ab}^\mu H_b^{(\bar{Q})} \right]$$

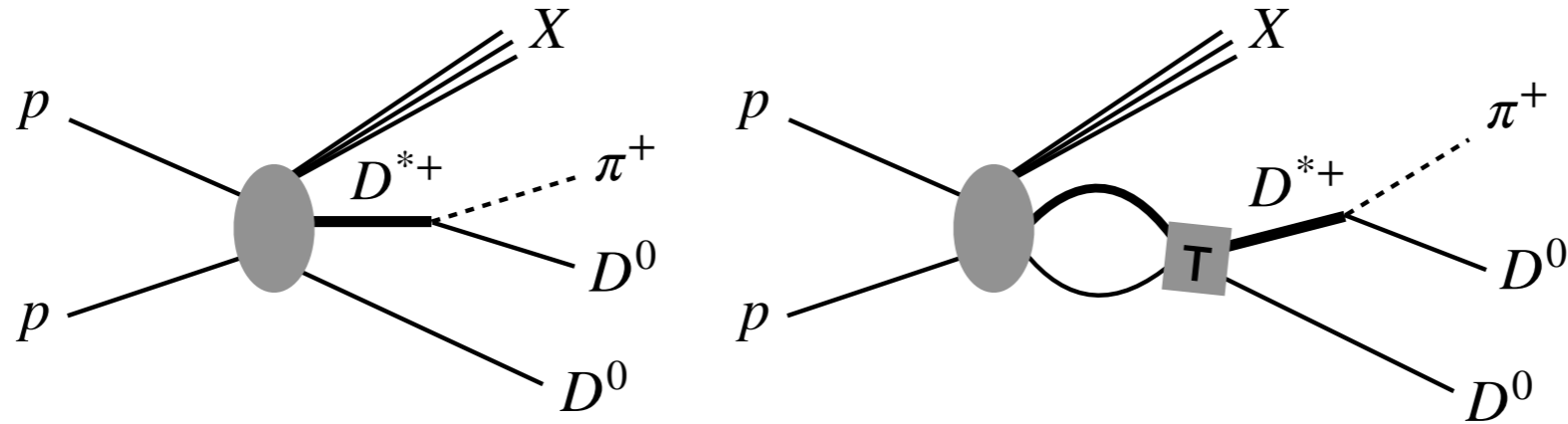
$$\mathcal{L}_{VH^{(\bar{Q})}H^{(\bar{Q})}} = -i\beta \text{Tr} \left[ \bar{H}_a^{(\bar{Q})} v_\mu (V_{ab}^\mu - \rho_{ab}^\mu) H_b^{(\bar{Q})} \right] \\ + i\lambda \text{Tr} \left[ \bar{H}_a^{(\bar{Q})} \sigma_{\mu\nu} F_{ab}^{\prime\mu\nu}(\rho) H_b^{(\bar{Q})} \right]$$

- $g = 0.57$  is determined by the strong decays  $D^* \rightarrow D\pi$ .
- undetermined  $\lambda$  &  $\beta$ .



# The inclusive production of the $T_{cc}$

$pp \rightarrow D^0(p_{D_1})D^0(p_{D_2})\pi^+(p_\pi)X$ ,  $X$  denotes all the other produced particles



The amplitude of the process

$$i\mathcal{M}_{pp \rightarrow DD\pi X} = \mathcal{A}_{pp \rightarrow DD^* X}^\mu \left\{ g_{\mu\alpha} - \frac{i}{(2\pi)^4} \int d^4 q_{D^*} G_{D^* \mu\nu}(q_{D^*}) G_D(p_{D_1} + p_{D_2} + p_\pi - q_{D^*}) T_\alpha^\nu(q_{D^*}, p_{D_1} + p_\pi) \right\} \\ \times G_{D^*}^{\alpha\beta}(p_{D_2} + p_\pi)(g p_{\pi,\beta}) + (p_{D_1} \rightarrow p_{D_2}),$$

The iso-vector and iso-scalar assignment for the  $\mathcal{A}$  with the production amplitudes satisfying

$$\mathcal{A}_{pp \rightarrow D^+ D^{0*} X}^\mu = \pm \mathcal{A}_{pp \rightarrow D^0 D^{*+} X}^\mu$$

➤ We can only find a satisfactory fit to the experimental data only in the **iso-scalar** case.

The T-matrix can be solved from the Lippmann-Schwinger equation

$$T(\vec{k}_{D^*}, \vec{k}'_{D^*}; E) = \mathcal{V}(\vec{k}_{D^*}, \vec{k}'_{D^*}; E) + \int d\vec{q} \frac{\mathcal{V}(\vec{k}_{D^*}, \vec{q}; E) T(\vec{q}, \vec{k}'_{D^*}; E)}{E - \sqrt{m_D^2 + q^2} - \sqrt{m_{D^*}^2 + q^2} + i\epsilon}$$

The effective potential is obtained with light-meson exchange potentials

$$\mathcal{V} = (V_\pi + V_{\rho/\omega}^t + V_{\rho/\omega}^u) \left( \frac{\Lambda^2}{\Lambda^2 + p_f^2} \right)^2 \left( \frac{\Lambda^2}{\Lambda^2 + p_i^2} \right)^2$$

with

$$V_\pi = \frac{g^2}{f_\pi^2} \frac{(q \cdot \epsilon_\lambda)(q \cdot \epsilon_{\lambda'}^\dagger)}{q^2 - m_\pi^2},$$

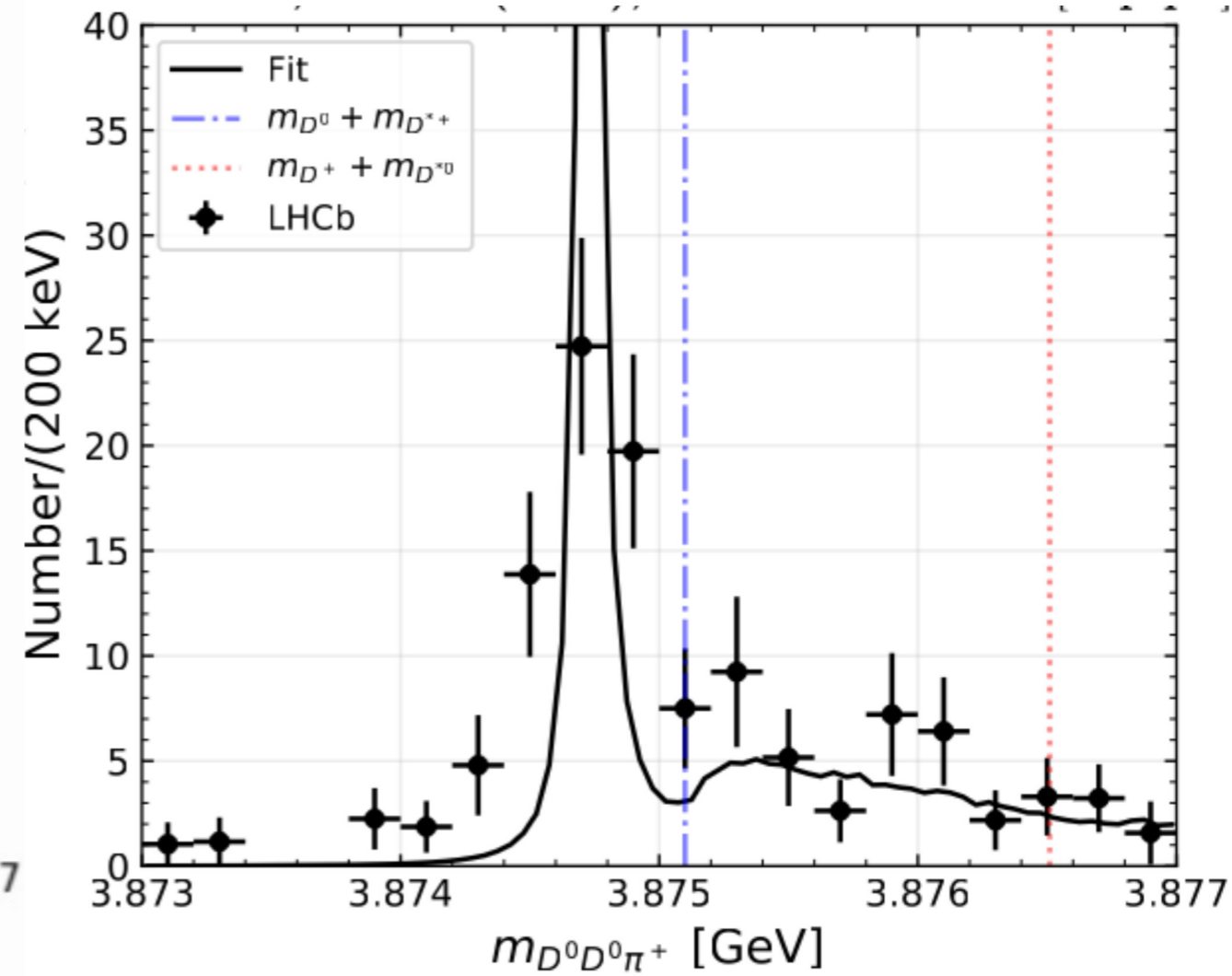
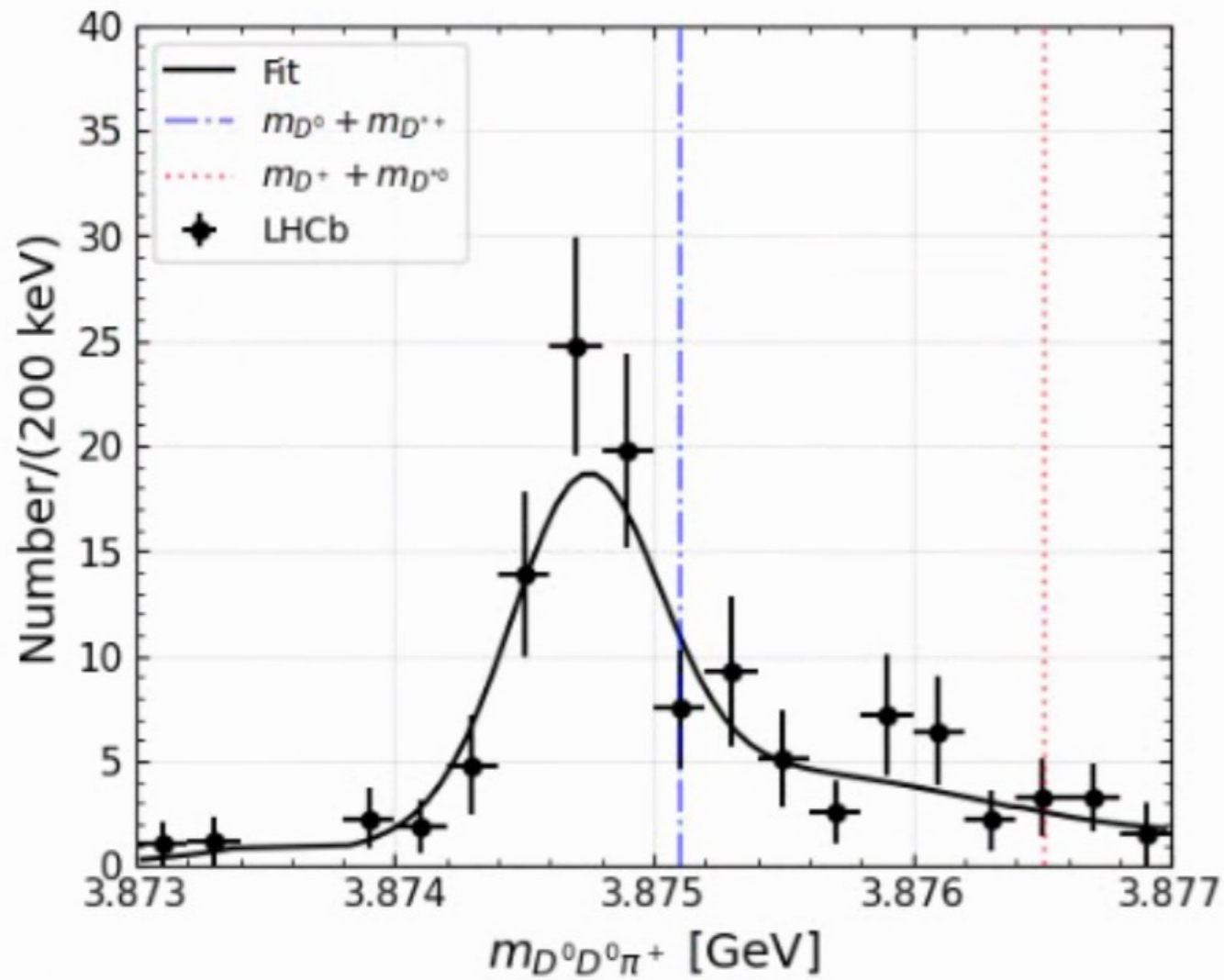
$$V_{\rho/\omega}^u = -2\lambda^2 g_V^2 \frac{(\epsilon_{\lambda'}^\dagger \cdot q)(\epsilon_\lambda \cdot q) - q^2(\epsilon_\lambda \cdot \epsilon_{\lambda'}^\dagger)}{q^2 - m_{\rho/\omega}^2},$$

$$V_{\rho/\omega}^t = \frac{\beta^2 g_V^2}{2} \frac{(\epsilon_\lambda \cdot \epsilon_{\lambda'}^\dagger)}{q^2 - m_{\rho/\omega}^2}.$$



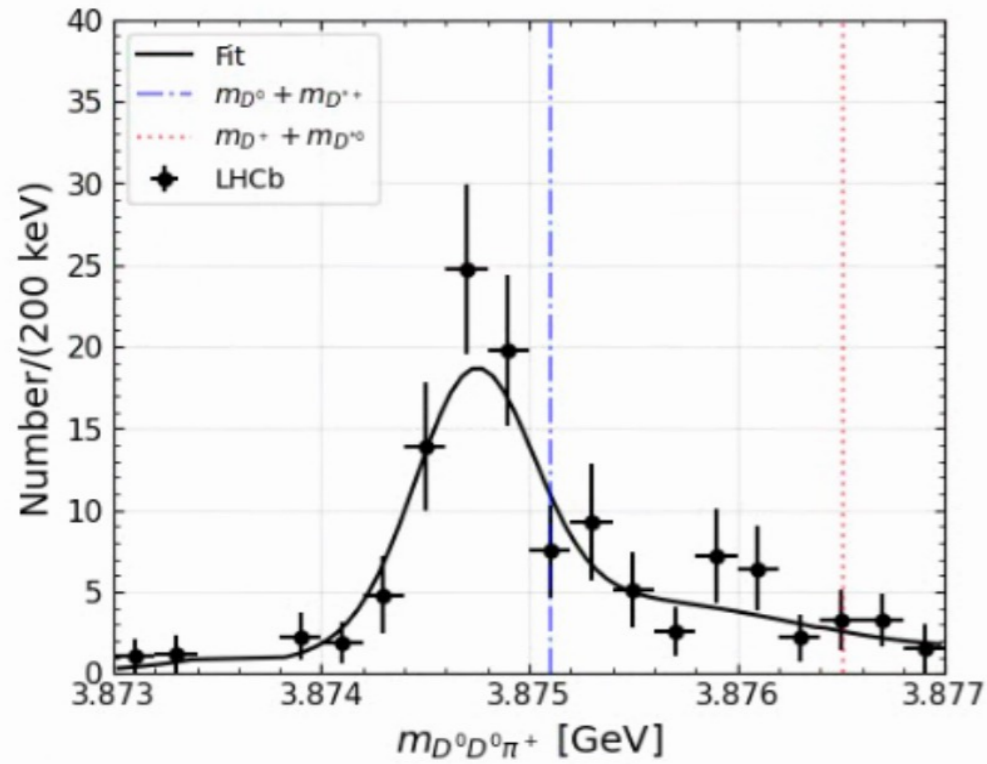
$\Lambda = 0.8 \text{ GeV}$ ,  $\chi^2/dof = 0.76$

Without resolution function

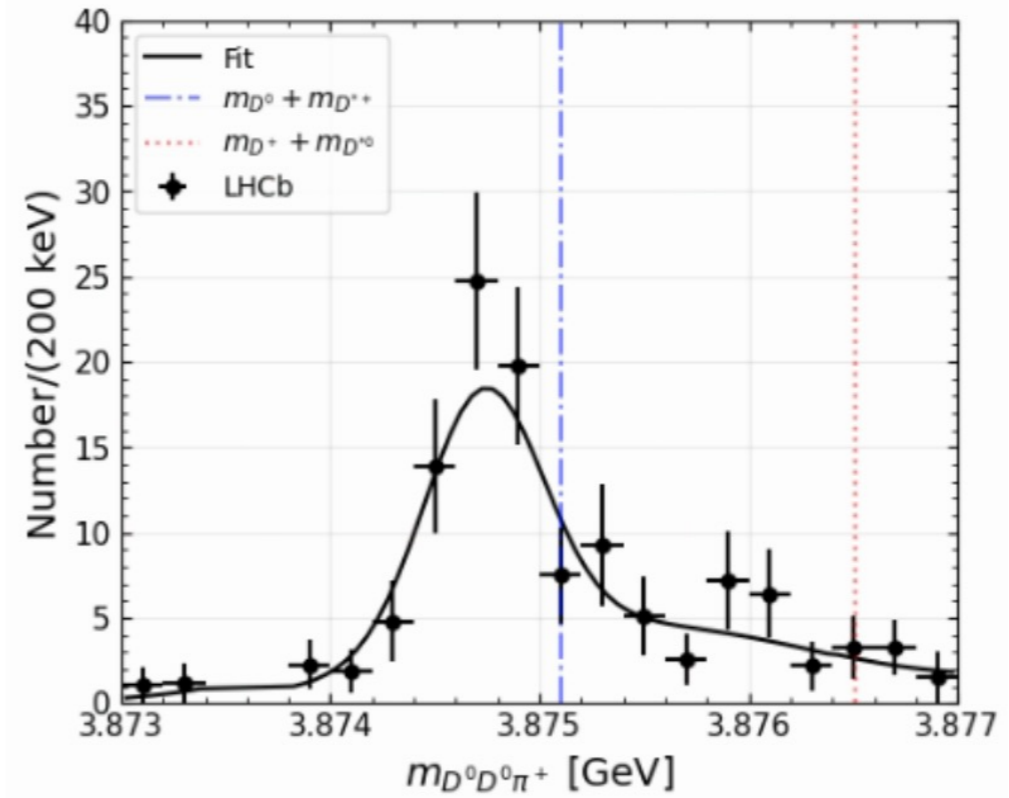


# Fitting result

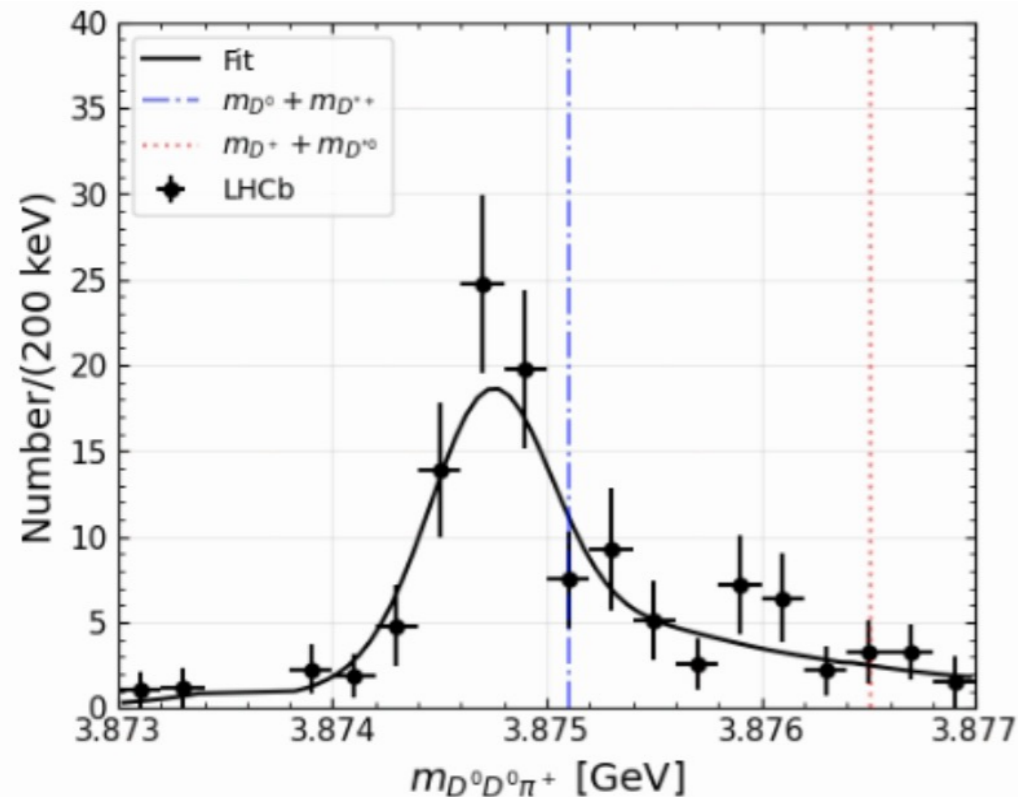
$\Lambda = 0.8 \text{ GeV}, \chi^2/dof = 0.76$



$\Lambda = 1.0 \text{ GeV}, \chi^2/dof = 0.76$



$\Lambda = 1.2 \text{ GeV}, \chi^2/dof = 0.78$



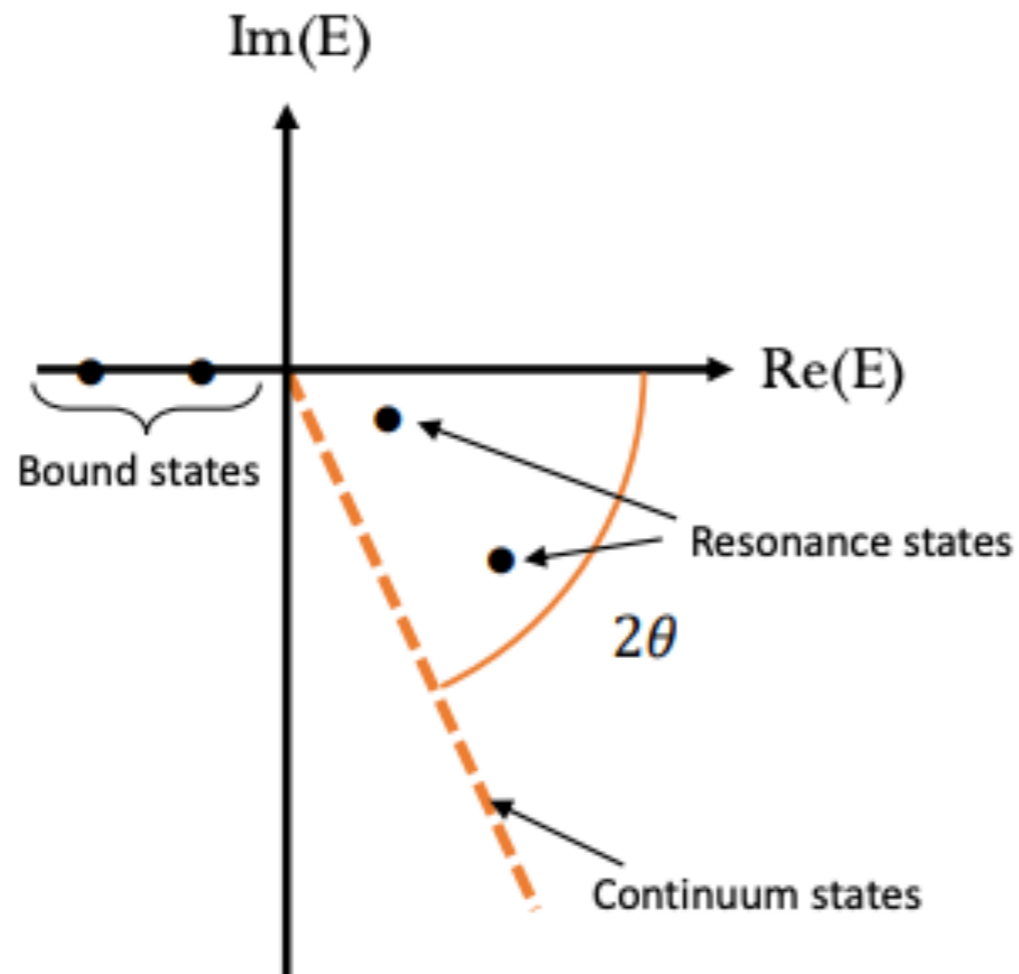
$\Lambda(\text{fixed})$	$\lambda$	$\beta$
0.8 GeV	$0.890 \pm 0.20$	$0.810 \pm 0.11$
1 GeV	$0.683 \pm 0.025$	$0.687 \pm 0.017$
1.2 GeV	$0.587 \pm 0.027$	$0.550 \pm 0.027$
1.17 GeV [1]	0.56	0.9

[1] Cheng, et al. Phys. Rev. D 106,016012 (2022).

The radius and momentum will rotate with an angle  $\theta$ :

$$\mathbf{r} \rightarrow \mathbf{r}e^{i\theta}, \quad \mathbf{q} \rightarrow \mathbf{q}e^{-i\theta}$$

$$H_\theta \Phi_\theta = E_\theta \Phi_\theta, \quad H_\theta = H(\mathbf{r}_\theta, \mathbf{q}_\theta) = \frac{q^2}{2u} e^{-2i\theta} + V(\mathbf{r}e^{i\theta}, \mathbf{q}e^{-i\theta})$$



S.Aoyama et al. PTP. 116, 1 (2006).  
T. Myo et al. PPNP. 79, 1 (2014)  
N. Moiseyev, Physics reports 302, 212 (1998)

With the varying  $\theta$ :

- the scattering states will rotate with  $2\theta$
- while the bound and resonant states will stay stable

# Results with $\Lambda = 0.8 \text{ GeV}$

- Only one pole appears—bound states

$$m_{T_{cc}} = 3874.7 \text{ MeV}, \Delta E = -387.7 \text{ keV}$$

$$\Gamma_{T_{cc}} = 67.3 \text{ keV}$$

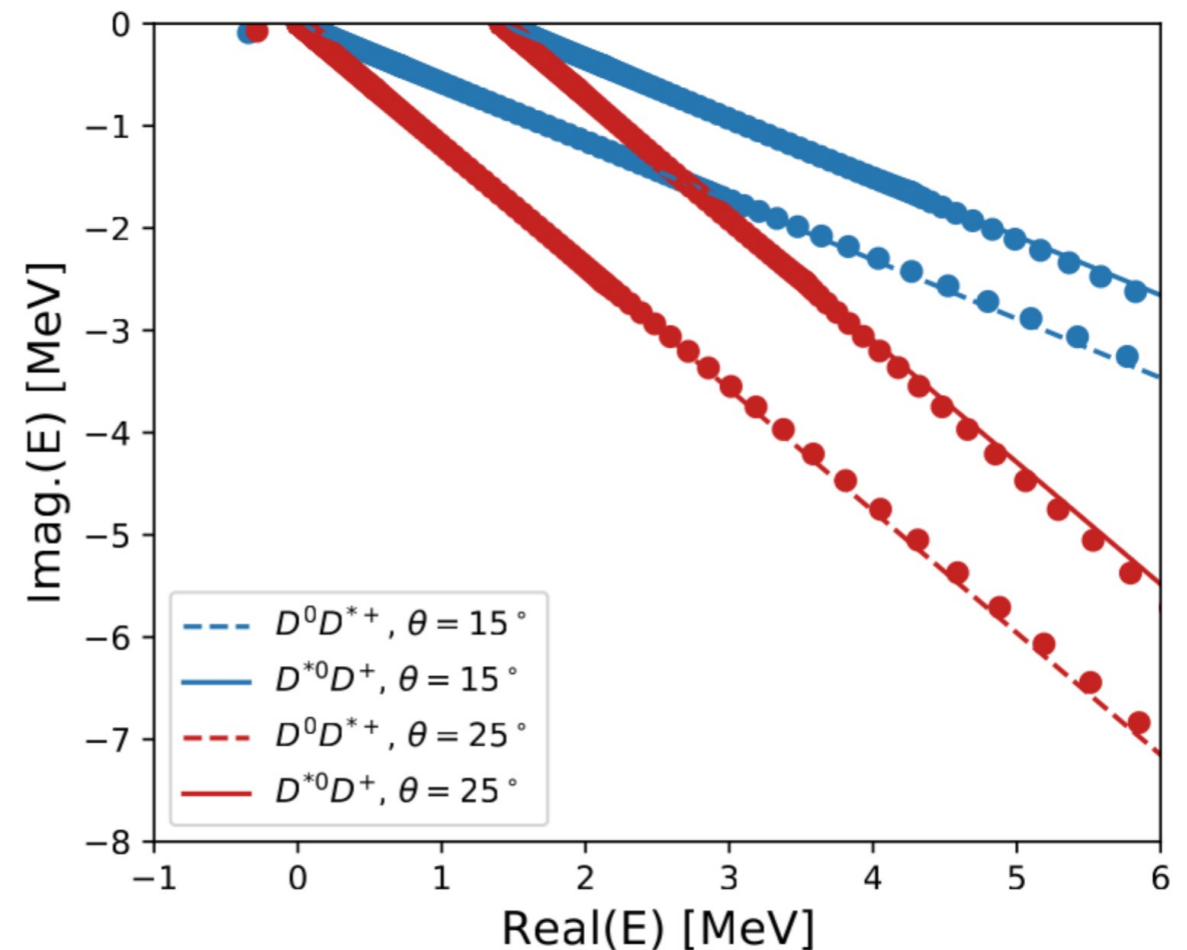
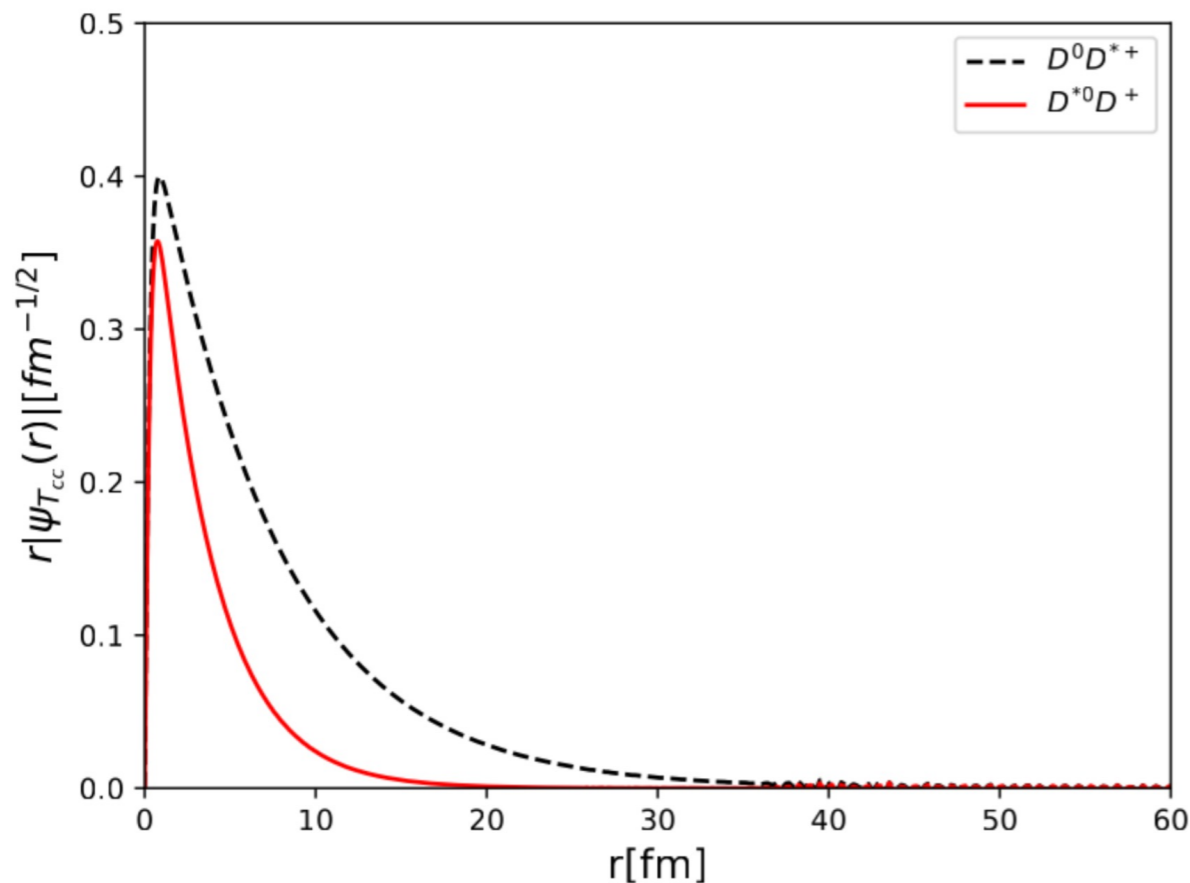
- $\sqrt{\langle r^2 \rangle} = 4.8 \text{ fm}$

- 70.1%  $D^{*+}D^0$ , 30%  $D^+D^{*0}$   $\longleftrightarrow$  95.8%,  $DD^*(I=0)$   
4.2%  $DD^*(I=1)$

$$[I=0] = \frac{1}{\sqrt{2}}(D^{*+}D^0 - D^{*0}D^+)$$

$$[I=1] = \frac{1}{\sqrt{2}}(D^{*+}D^0 + D^{*0}D^+)$$

Mass differences of  $D^{*+}D^0$  and  $D^+D^{*0}$



# Results with three $\Lambda$



$\Lambda$ (GeV)	BE (keV)	$\Gamma$ (keV)	$\sqrt{\langle r^2 \rangle}$	$I = 0$	$I = 1$	$P(D^0 D^{*+})$	$P(D^+ D^{*0})$	$\frac{\text{Res}(D^0 D^{*+})}{\text{Res}(D^+ D^{*0})}$
0.8	-387.7	67.3	4.8 fm	95.8%	4.2%	70.0%	30.0%	$-1.063 + 0.001I$
1.0	-393.0	70.4	4.7 fm	95.8%	4.2%	70.0%	30.0%	$-1.055 + 0.001I$
1.2	-391.6	72.7	4.7 fm	95.7%	4.3%	70.3%	29.7%	$-1.052 + 0.001I$

- The conclusion remains the same using the three different cutoff values.
- The binding energy of the bound state is around  $\Delta E \sim -390\text{keV}$ , which is consistent

with that of the measurement ( $\Delta E_{\text{exp}} = -360(40)\text{keV}$ ).

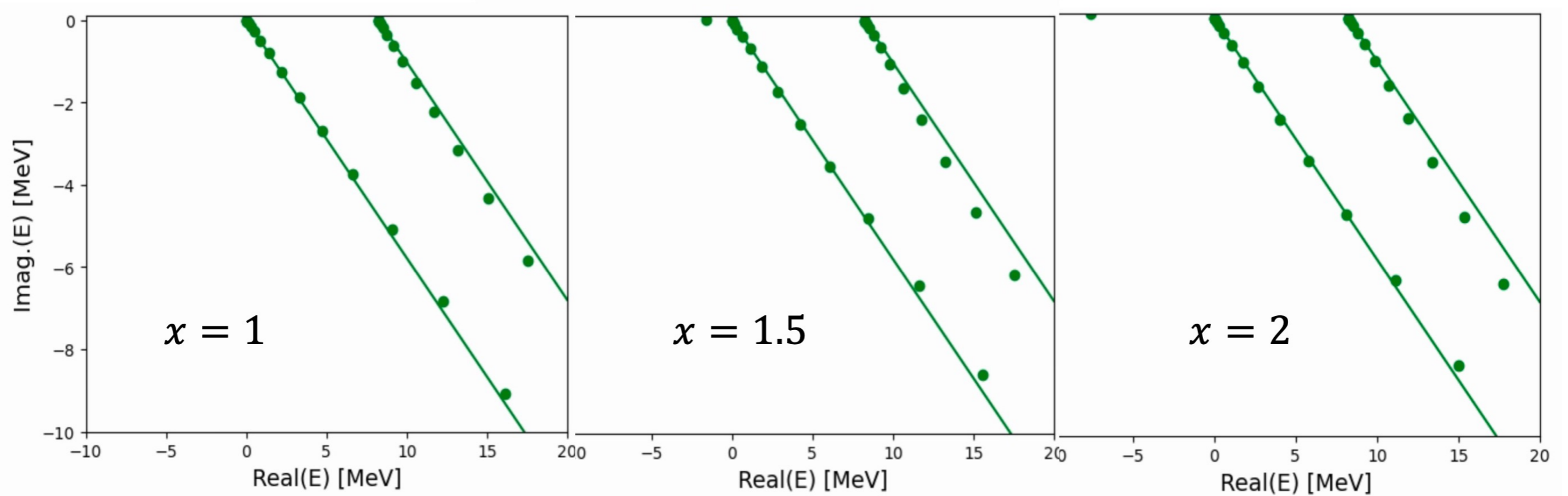
LHCb, Nature Commun. 13 (2022) 1, 3351



# Direct application to $D\bar{D}^*$ : $X(3872)$



- Without the  $c\bar{c}$  core, there are no bound states.
- $V'_{D\bar{D}^*} = x * V_{D\bar{D}^*}$



*$D\bar{D}^*$  interaction is attractive but not strong enough to form a bound state.*



*Inclusion of  $c\bar{c}$  core*

# $X(3872) : D\bar{D}^* + c\bar{c}$

- The  $D\bar{D}^*$  system with quantum number  $I(J^{PC}) = 0(1^{++})$  can couple with the  $\chi_{c1}(2P)$ .
- The coupled channel effect between them can be described by the quark-pair-creation model:

$$g_{D\bar{D}^*,c\bar{c}}(|\vec{k}_{D\bar{D}^*}|) = \gamma I_{D\bar{D}^*,c\bar{c}}(|\vec{k}_{D\bar{D}^*}|)$$

where  $\vec{k}_{D\bar{D}^*}$  is the relative momentum in the  $D\bar{D}^*$  channel.

$I_{D\bar{D}^*,c\bar{c}}(|\vec{k}_{D\bar{D}^*}|)$  is the overlap of the meson wave functions ← GI quark model

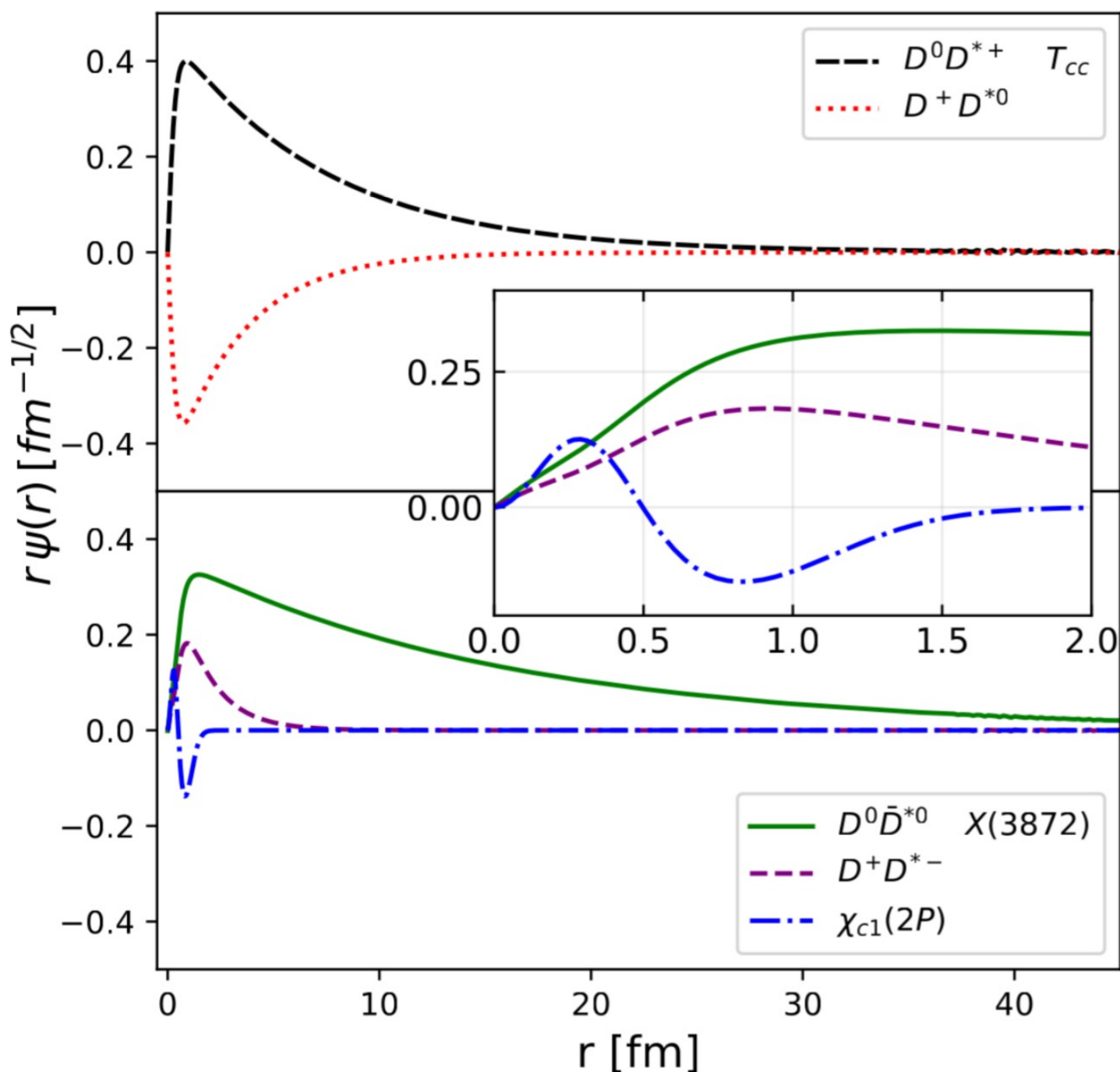
- $\gamma$  is determined to reproduce the  $\psi(3770)$ :

$$\gamma = 4.69$$

- The the X(3872) can be obtained:

$X(3872)$	BE (keV)	$\Gamma$ (keV)	$\sqrt{\langle r^2 \rangle}$	$I = 0$	$I = 1$	$P(D^0\bar{D}^{*0})$	$P(D^+D^{*-})$	$P(c\bar{c})$
	-80.4	32.5	11.2 fm	71.9%	28.1%	94.0%	4.8%	1.2%

Wave functions of  $T_{cc}$  and X(3872)



- Long tails for the radius distribution.

- X(3872) has a even longer tails than  $T_{cc}$

✓  $r < 2$  fm,  $c\bar{c} + \bar{D}D^*$  are important.

✓  $r < 0.5$  fm,  $c\bar{c}$  core dominates.

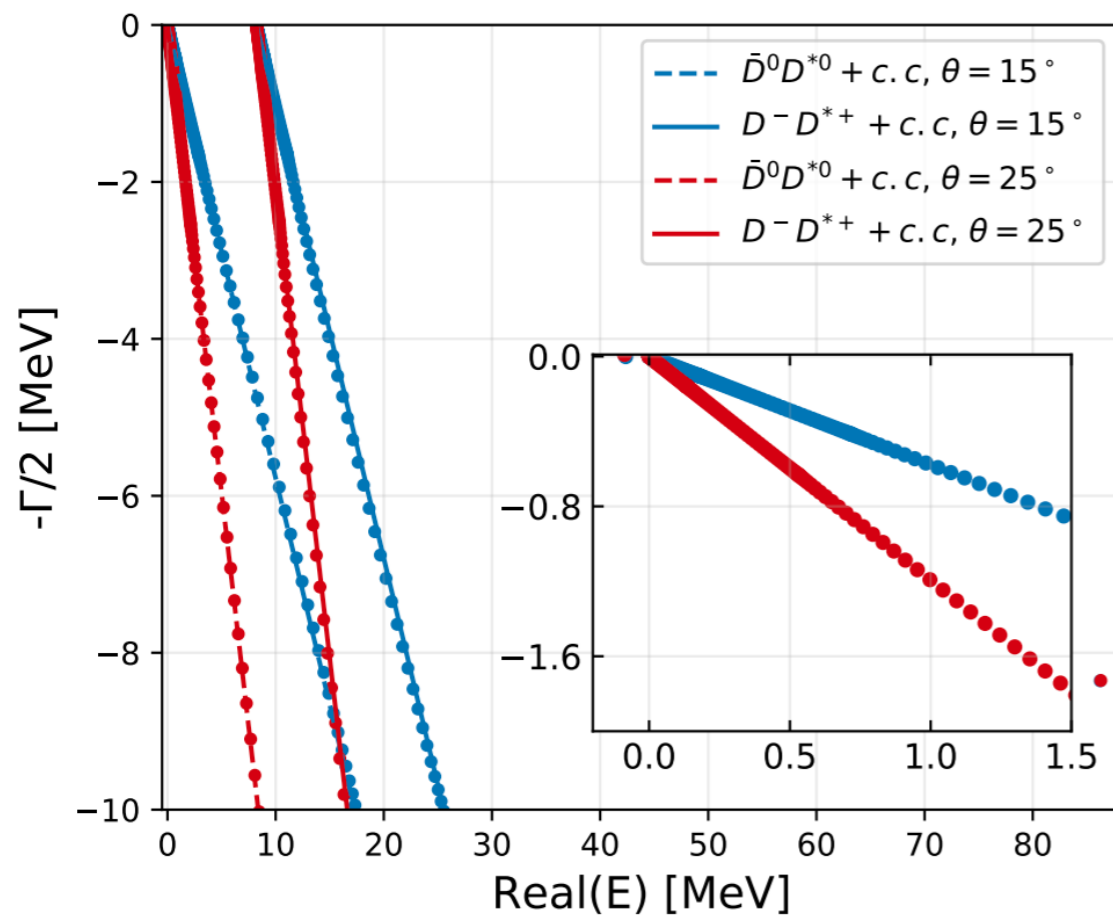
✓  $D\bar{D}^*$  plays the dominant role in the long-distance region, which contributes to  $\sqrt{\langle r^2 \rangle}$ .

# Direct application to $D\bar{D}^*$ : Candidate for X(3940)?

- Besides the X(3872), we also find a signal of the resonant state  $\chi_{c1}(2P)$  with

$$M = 3957.9\text{MeV}, \Gamma = 16.7\text{MeV},$$

which might be related to the X(3940) observed in the  $D\bar{D}^*$  channel.



X(3940) MASS

$3942 \pm 9 \text{ MeV}$

X(3940) WIDTH

$37^{+27}_{-17} \text{ MeV}$

## X(3940) Decay Modes

	Mode	Fraction ( $\Gamma_i / \Gamma$ )
$\Gamma_1$	$D\bar{D}^* + c.c.$	seen

# Compare with the lattice results



Ours:  $\chi_{c1}(2P) \rightarrow M = 3957.9\text{MeV}$

Haozheng Li et al, arXiv: 2402.14541

$m_\pi(\text{MeV})$	250(3)	307(2)	362(1)	417(1)
$m_R(\text{MeV})$	3924(5)	3926(6)	3969(4)	3995(4)
$\Gamma_R(\text{MeV})$	63(23)	57(18)	37(13)	57(10)

$X \approx 1$  and indicates a predominant  $D\bar{D}^*$  component. This state may correspond to  $X(3872)$ . On the other hand, our results of the finite volume energies also hint at the existence of a  $1^{++}$  resonance below 4.0 GeV with a width around 60 MeV.



# Compare with the experimental results



Ours: virtual state with  $1^{+-}$  and  $M = 3870.2$  MeV

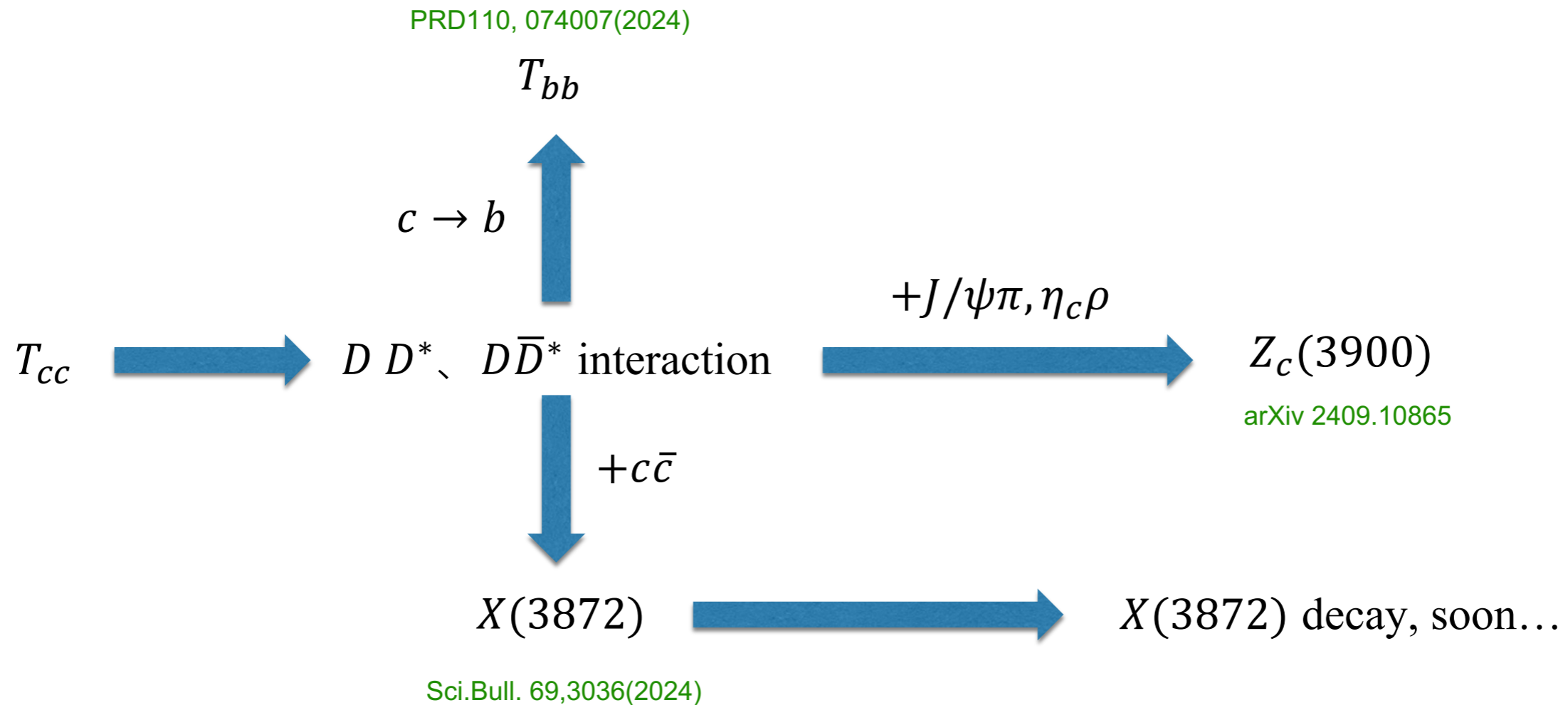
COMPASS:  $\tilde{X}(3872)$  with  $M = 3860.0 \pm 10.4$  MeV COMPASS, PLB783,334

Ours:  $h_c(2P) \rightarrow M = 3961.3$  MeV

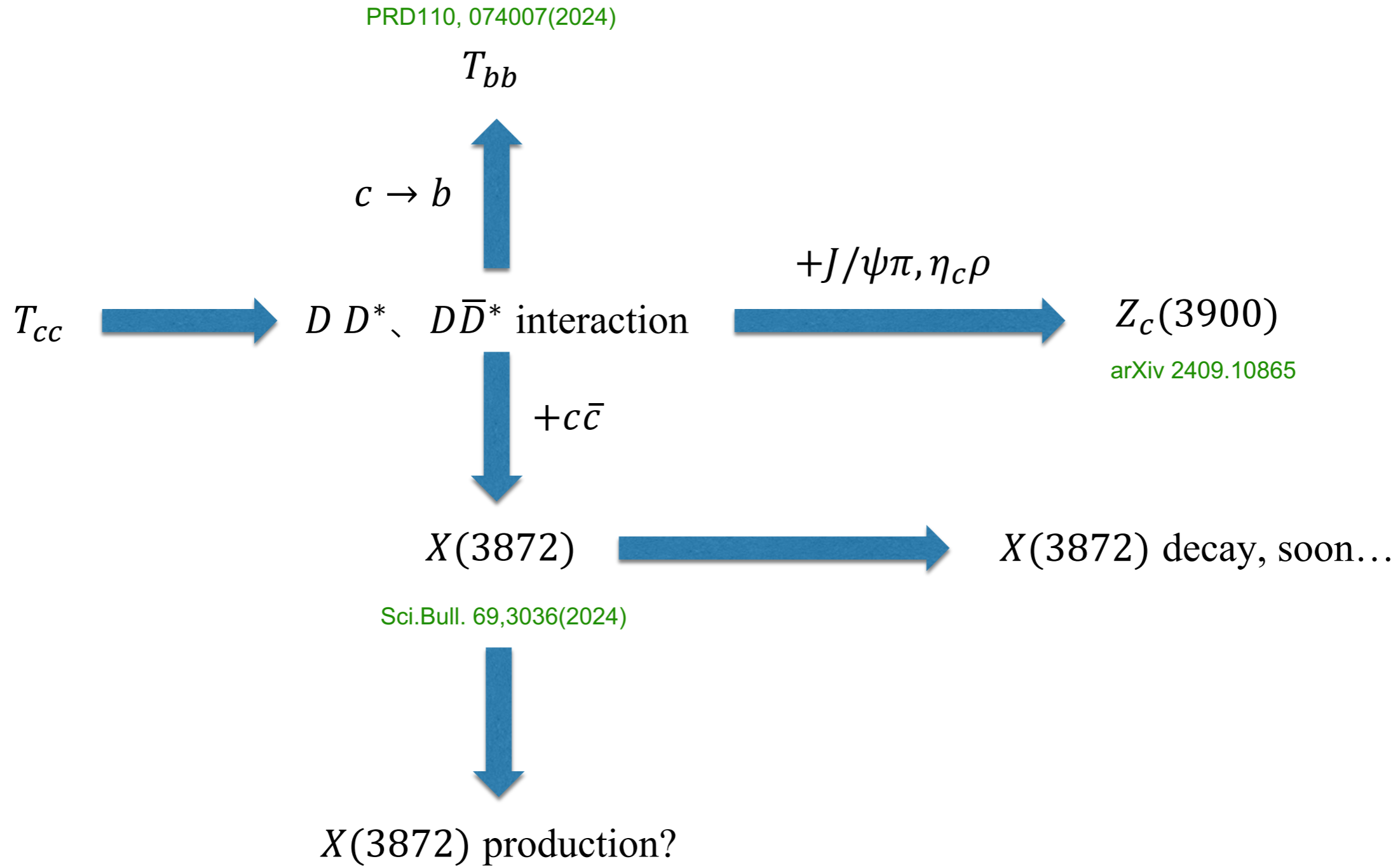
$\chi_{c1}(2P) \rightarrow M = 3957.9$  MeV

LHCb, arXiv:2406.03156

This work		Known states <span style="border: 1px solid green; padding: 2px;">[6]</span>		$c\bar{c}$ prediction <span style="border: 1px solid green; padding: 2px;">[34]</span>
$\eta_c(3945)$	$J^{PC} = 0^{-+}$	$X(3940)$ <span style="border: 1px solid green; padding: 2px;">[9]</span> <span style="border: 1px solid green; padding: 2px;">[10]</span>	$J^{PC} = ?^{??}$	$\eta_c(3S)$ $J^{PC} = 0^{-+}$
$m_0 = 3945^{+28}_{-17}{}^{+37}_{-28}$	$\Gamma_0 = 130^{+92}_{-49}{}^{+101}_{-70}$	$m_0 = 3942 \pm 9$	$\Gamma_0 = 37^{+27}_{-17}$	$m_0 = 4064$ $\Gamma_0 = 80$
$h_c(4000)$	$J^{PC} = 1^{+-}$	$T_{c\bar{c}}(4020)^0$ <span style="border: 1px solid green; padding: 2px;">[35]</span>	$J^{PC} = ?^{?-}$	$h_c(2P)$ $J^{PC} = 1^{+-}$
$m_0 = 4000^{+17}_{-14}{}^{+29}_{-22}$	$\Gamma_0 = 184^{+71}_{-45}{}^{+97}_{-61}$	$m_0 = 4025.5^{+2.0}_{-4.7} \pm 3.1$	$\Gamma_0 = 23.0 \pm 6.0 \pm 1.0$	$m_0 = 3956$ $\Gamma_0 = 87$
$\chi_{c1}(4010)$	$J^{PC} = 1^{++}$			$\chi_{c1}(2P)$ $J^{PC} = 1^{++}$
$m_0 = 4012.5^{+3.6}_{-3.9}{}^{+4.1}_{-3.7}$	$\Gamma_0 = 62.7^{+7.0}_{-6.4}{}^{+6.4}_{-6.6}$			$m_0 = 3953$ $\Gamma_0 = 165$



- $T_{cc}$  is used to fix the  $D\bar{D}^*$  interactions in  $X(3872)$ .
- Short-range interactions and structures of  $X(3872)$  should be studied by considering the  $c\bar{c}$  core.



- What important role the  $c\bar{c}$  core can play in the production of the  $X(3872)$ ?

The probability of the  $c\bar{c}$  component in the  $X(3872)$  can be obtained from fitting its production:

$$d\sigma(pp \rightarrow X(J/\psi\pi^+\pi^-)) = d\sigma(pp \rightarrow \chi'_{c1}) \cdot k, \quad k = Z_{c\bar{c}} \cdot Br_0$$

$$\longrightarrow Z_{c\bar{c}} = (28-44)\%$$

C. Meng, H. Han, K.T. Chao, Phys. Rev. D 96, 074014

**Thank you !**