



Testing Gravity Theories with Pulsars

Kavli Institute for Astronomy and Astrophysics

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交叉学科理论研究中心

Kavli Institute for Astronomy and Astrophysics

- KIAA (2006-now) is jointly supported by **Peking University** and an endowment by **Kavli Foundation**
 - 1 Observational cosmology, galaxy formation and evolution
 - 2 Interstellar medium, star formation, and planets
 - 3 **Gravitational physics and high-energy phenomena**
 - 4 Computational astrophysics



Outline

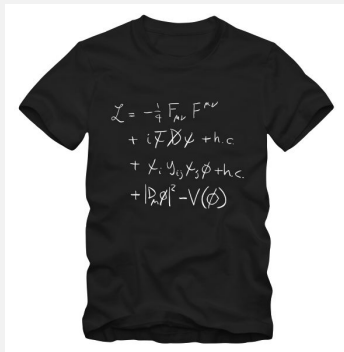
- 1 Introduction to Gravity Tests**
- 2 Binary Pulsar Timing**
- 3 Strong Field Gravity**
- 4 Massive Gravity**
- 5 Fifth Force from Dark Matters**
- 6 Summary**

1. Introduction to Gravity Tests

Modern Physics Landscape

■ Standard Model

quantum field theory



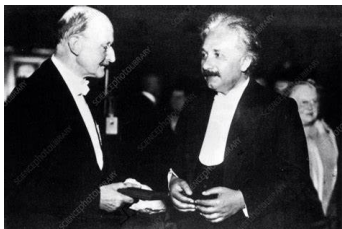
■ General Relativity

gravitation and spacetime



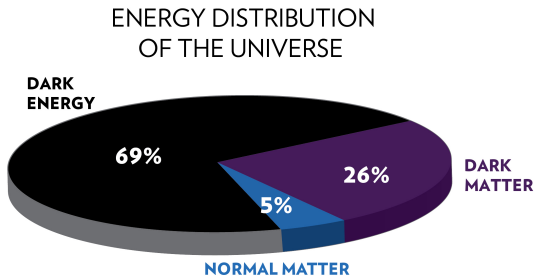
Absence of Quantum Gravity

- On one hand, we have **Quantum Field Theory** to describe the electromagnetic, strong, and weak interactions
- On the other hand, we have **General Relativity** to describe the gravity, as the dynamics of curved spacetime
- However, QFT and GR are **Not Compatible** with each other!



[Planck & Einstein]

Pathways to New Physics?



Dark energy? Dark matter?
Inflation? Heavy W boson?
Neutrino mass? ...





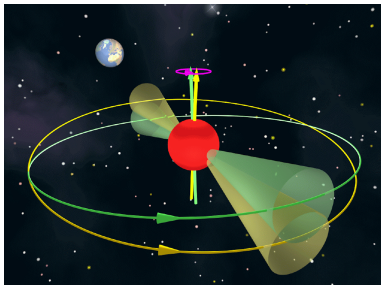
**Theoretical physics is beautiful,
but not yet complete**

**Gravity may be holding
the key**

2. Binary Pulsar Timing

Pulsars

- Pulsars are rotating magnetized neutron stars
- Due to their large moment of inertia and small external torque, their rotation is extremely stable \Rightarrow lighthouse



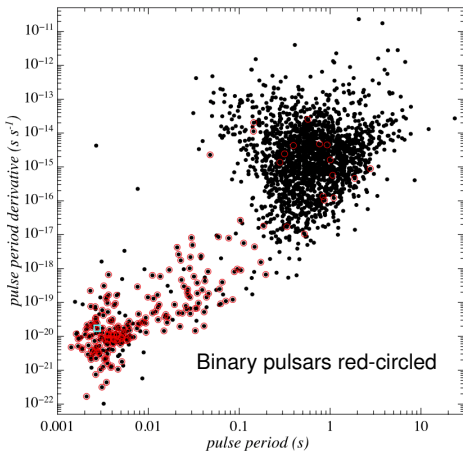
Pulsars are clocks

Pulsars are **precision** clocks

PSR J0737–3039A: $\nu = 44.05406864196281(17)$ Hz

(16 significant digits!)

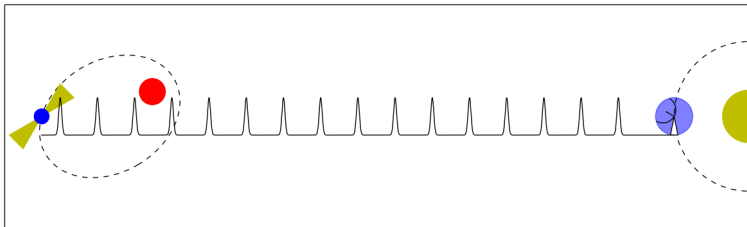
Pulsar Populations



Manchester et al. 2005 [[arXiv:astro-ph/0412641](https://arxiv.org/abs/astro-ph/0412641)]; Wex & Kramer 2020

Pulsar Timing

- Large radio telescopes are used to record the **times of arrival** of pulses, which are affected by
 - Solar dynamics
 - Binary motion
 - Interstellar medium

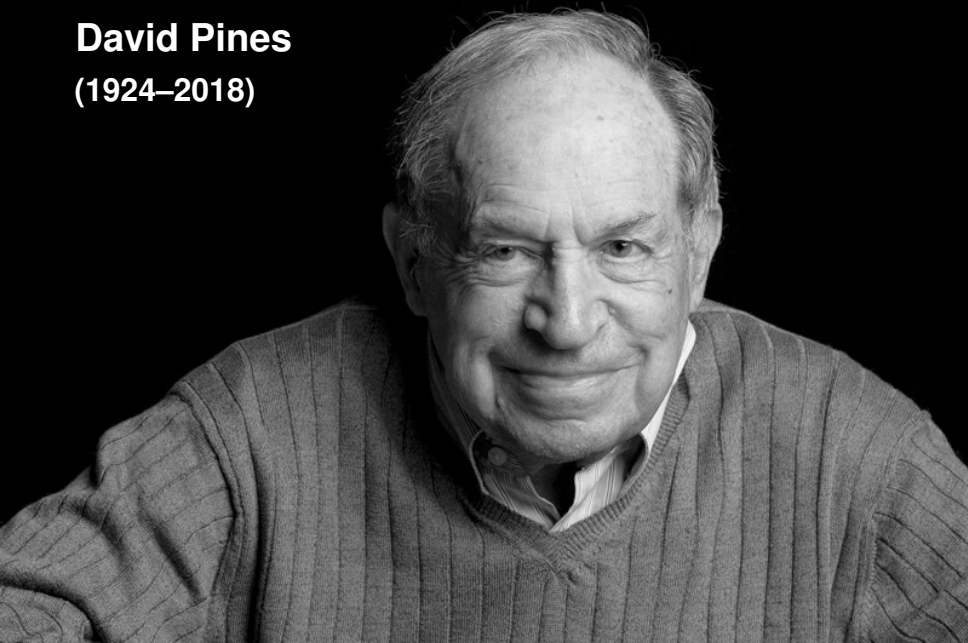


Five-hundred-meter Aperture Spherical Telescope (FAST)



David Pines

(1924–2018)



Pines Theorem: “NSs are *superstars*”

NSs' *Superproperties*

cf. Riccardo Ciolf's PhD thesis

They are indeed *superdense* ($\bar{\rho} \gtrsim 2.8 \times 10^{14} \text{ g cm}^{-3}$), endowed with *superstrong* gravity (in need of GR). They are *superfast* rotators ($\nu \sim 716 \text{ Hz}$) and *superprecise* timers (in need of $\gtrsim 10$ digits), but also *superglitching* objects. NS matter is partially *superconducting* and/or *superfluid*. NSs possess *superstrong* magnetic fields (up to $B \gtrsim 10^{15} \text{ G}$). In addition, NSs are *superrich* in the Physics involved (all four fundamental forces; Nuclear & Particle & Condensed Matter & Plasma & Magnetohydrodynamics & GR & Radio/Optical/X-ray/ γ -ray & Neutrino & GW Physics etc.). ...and they are born in *supernovae*!



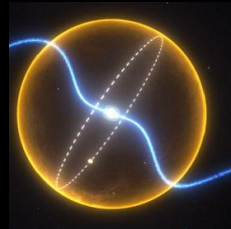
Perspective

Neutron stars as extreme laboratories for gravity tests

Lijing Shao^{a,b,*}, Kent Yagi^{c,1}

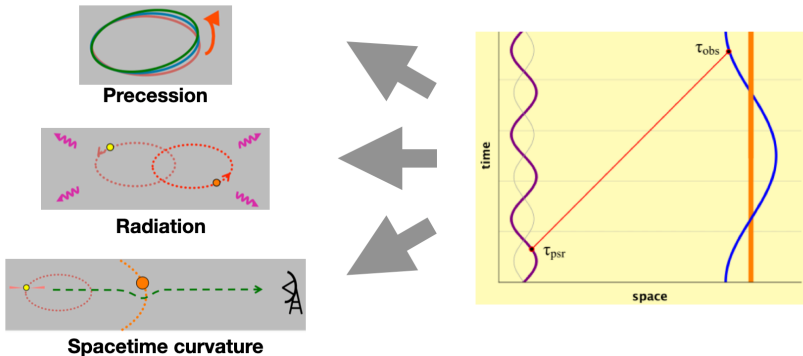
Pulsars are *truly* **Extreme Laboratories**

- strong gravity
- dense nuclear matters
- unique astrophysics
- ...



Binary Pulsars

- Binary pulsars are sensitive to effects beyond the Newtonian gravity



Precision Astrophysics (Kramer 2016)

Masses:

Masses of neutron stars:

$$m_1 = 1.4398(2) M_{\odot}$$

$$m_2 = 1.3886(2) M_{\odot}$$

Mass of WD companion:

$$0.207(2) M_{\odot}$$

Mass of millisecond pulsar:

$$1.67(2) M_{\odot}$$

Main sequence star companion:

$$1.029(8) M_{\odot}$$

Mass of Jupiter and moons:

$$9.547921(2) \times 10^{-4} M_{\odot}$$

Spin parameters:

Period:

$$5.757451924362137(2) \text{ ms}$$

Orbital parameters:

Period:

$$0.102251562479(8) \text{ day}$$

Eccentricity:

$$3.5(1.1) \times 10^{-7}$$

Astrometry:

Distance:

$$157(1) \text{ pc}$$

Proper motion:

$$140.915(1) \text{ mas yr}^{-1}$$

Tests of general relativity:

Periastron advance:

$$4.226598(5) \text{ deg yr}^{-1}$$

Shrinkage due to GW emission:

$$7.152(8) \text{ mm/day}$$

GR validity (obs/exp):

$$1.0000(5)$$

Constancy of grav. Constant, \dot{G}/G :

$$-0.6(1.6) \times 10^{-12} \text{ yr}^{-1}$$

Post-Keplerian Parameters

$$\dot{\omega} = 3 \left(\frac{P_b}{2\pi} \right)^{-5/3} (T_{\odot} M)^{2/3} (1 - e^2)^{-1}$$

$$\gamma = e \left(\frac{P_b}{2\pi} \right)^{1/3} T_{\odot}^{2/3} M^{-4/3} m_B (m_A + 2m_B)$$

$$\dot{P}_b = -\frac{192\pi}{5} \left(\frac{P_b}{2\pi} \right)^{-5/3} \left(1 + \frac{73}{24} e^2 + \frac{37}{96} e^4 \right) (1 - e^2)^{-7/2} T_{\odot}^{5/3} m_A m_B M^{-1/3}$$

$$r = T_{\odot} m_B$$

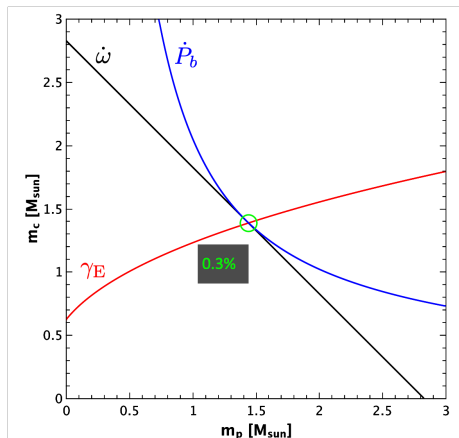
$$s = x \left(\frac{P_b}{2\pi} \right)^{-2/3} T_{\odot}^{-1/3} M^{2/3} m_B^{-1}$$

$$\delta_r = T_{\odot}^{2/3} \left(\frac{P_b}{2\pi} \right)^{-2/3} M^{-4/3} (3m_A^2 + 6m_A m_B + 2m_B^2)$$

$$\delta_{\theta} = T_{\odot}^{2/3} \left(\frac{P_b}{2\pi} \right)^{-2/3} M^{-4/3} \left(\frac{7}{2} m_A^2 + 6m_A m_B + 2m_B^2 \right)$$

Damour & Deruelle 1985, 1986; Damour & Taylor 1992

The Hulse-Taylor Pulsar B1913+16



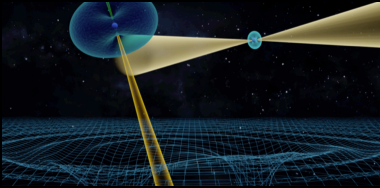
Nobel Prize in Physics 1993

Hulse & Taylor 1975; Weisberg & Huang 2016



Double Pulsar

The Double Pulsar J0737–3039A/B

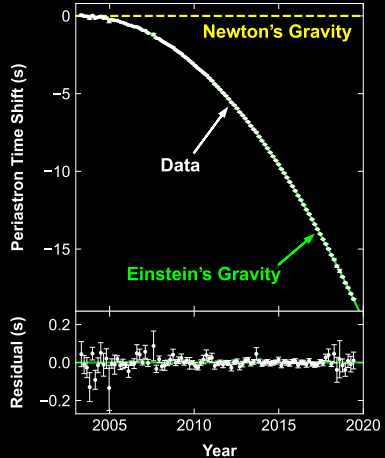


Physics VIEWPOINT

General Relativity Withstands Double Pulsar's Scrutiny

Sixteen years of timing data from the double pulsar confirm the validity of Einstein's theory of general relativity to a new level.

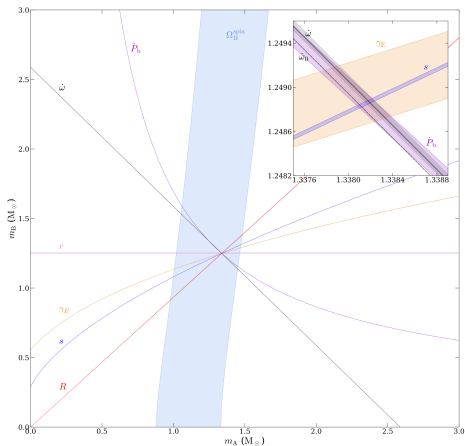
By Lijing Shao



In GR, observations of Double Pulsar agree within 0.01%

Kramer et al. 2021 [[arXiv:2112.06795](https://arxiv.org/abs/2112.06795)]

The Double Pulsar J0737–3039A/B



Double Pulsar passed a few tests of GR *simultaneously*

Breton et al. 2008 [[arXiv:0807.2644](https://arxiv.org/abs/0807.2644)]; Kramer et al., 2021 [[arXiv:2112.06795](https://arxiv.org/abs/2112.06795)]

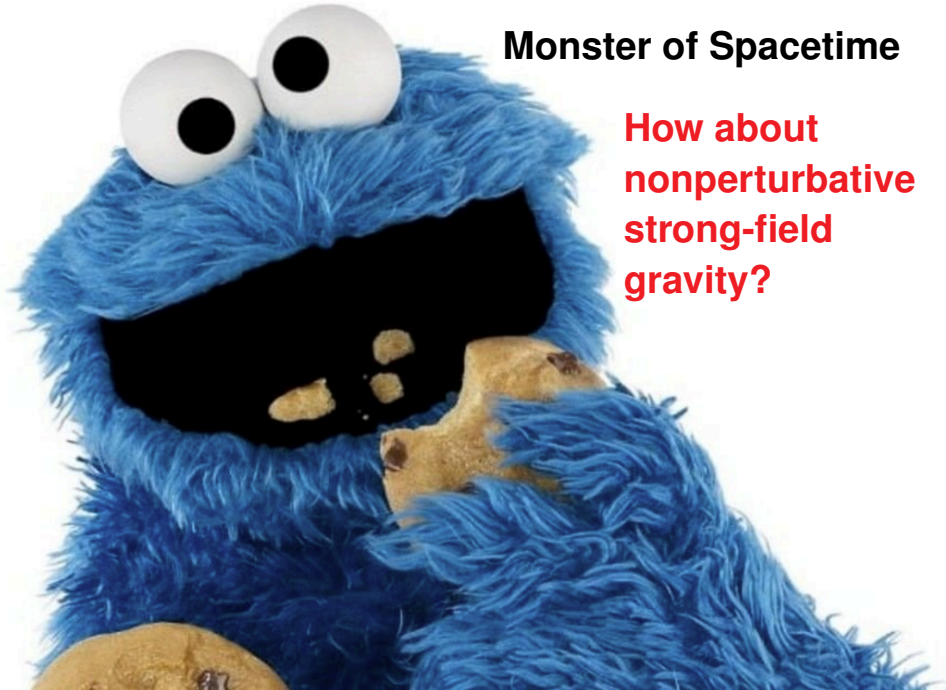
Sensitive to tiny changes in orbits

**Binary pulsars are
excellent testbeds of
gravity theories**

3. Strong Field Gravity

Precision clocks in curved spacetime

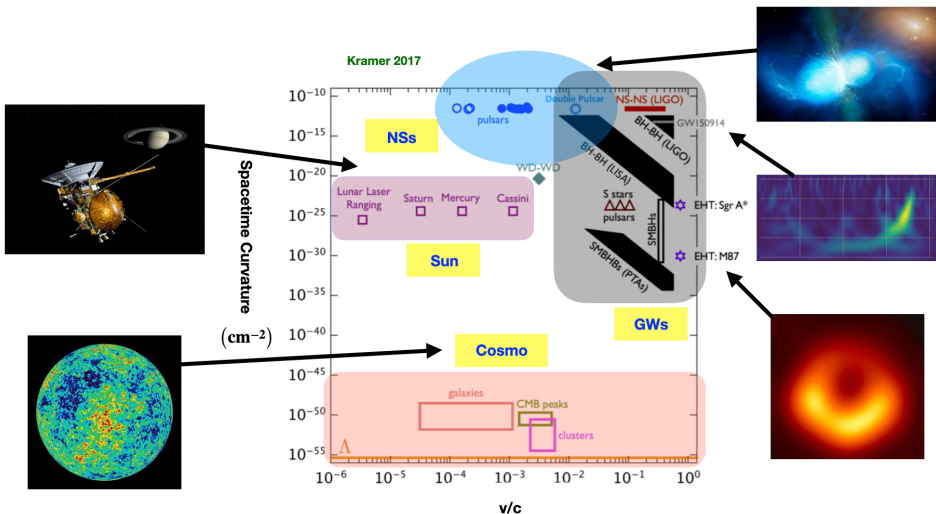




Monster of Spacetime

How about
nonperturbative
strong-field
gravity?

Parameter Space in Gravity Tests



Scalar-Tensor Gravity

$$S = \frac{c^4}{16\pi G_*} \int \frac{d^4x}{c} \sqrt{-g_*} [R_* - 2g_*^{\mu\nu} \partial_\mu \varphi \partial_\nu \varphi - V(\varphi)] + S_m [\psi_m; A^2(\varphi) g_{\mu\nu}^*]$$

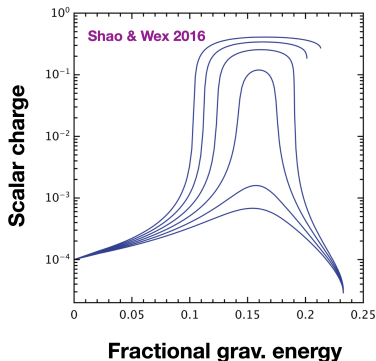
- **Example** A class of cosmologically well-motivated scalar-tensor theories $T(\varphi_0, \beta_0)$, that are solely described by two theory parameters: φ_0 & β_0

$$V(\varphi) = 0$$

$$A(\varphi) = \exp\left(\beta_0 \varphi^2 / 2\right)$$

Damour & Esposito-Farèse 1992; 1993; 1996 [arXiv:gr-qc/9602056]

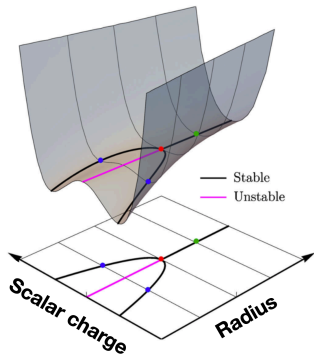
Scalar-Tensor Gravity



Nonperturbative **spontaneous scalarization**
could happen for isolated NSs

Damour & Esposito-Farèse 1992; 1993; 1996 [[arXiv:gr-qc/9602056](https://arxiv.org/abs/gr-qc/9602056)]

Scalar-Tensor Gravity



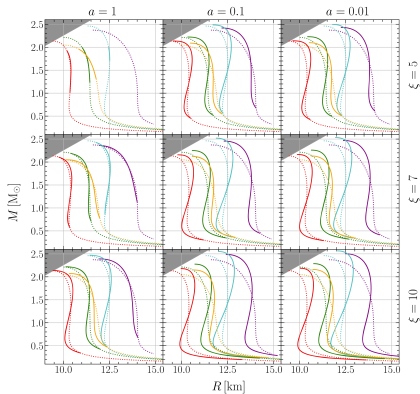
Strong-field behavior is analogous to **Landau's phase transition** after a critical point

Damour & Esposito-Farèse 1996 [[arXiv:gr-qc/9602056](#)]

Esposito-Farèse 2004 [[arXiv:gr-qc/0409081](#)]; Sennett et al. 2017 [[arXiv:1708.08285](#)]

Massive Scalar-Tensor Gravity

- When a mass term is included, say $V(\varphi) \sim m^2\varphi^2$, a Yukawa-type suppression happens for the deviation

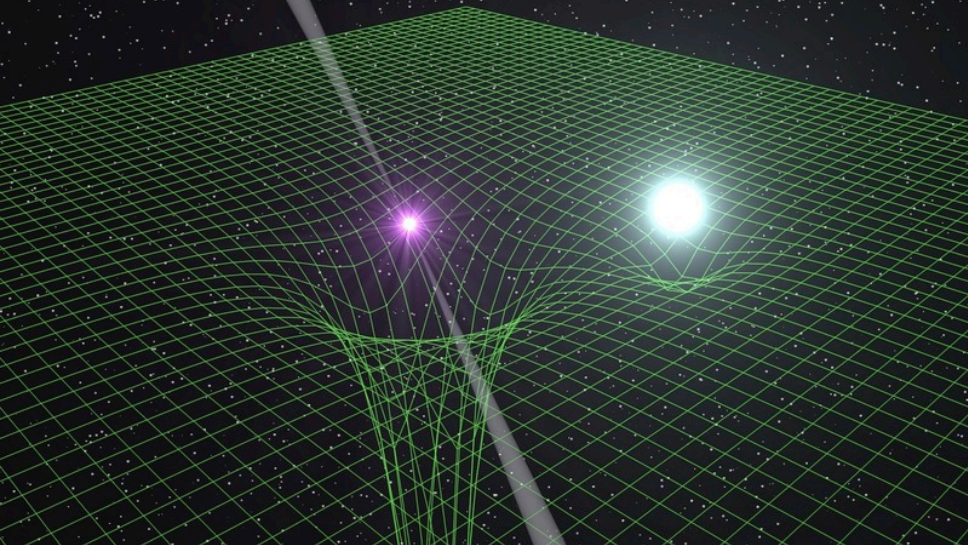


Ramazanoğlu & Pretorius 2016; Yazadjiev, Doneva, Popchev 2016; Xu, Gao, Shao 2020

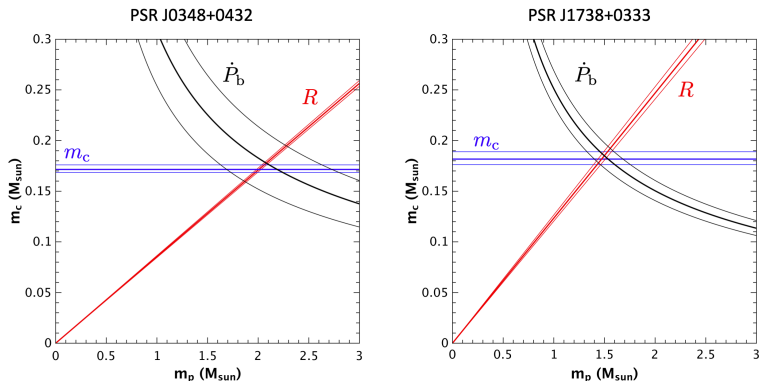
Strong-field gravity can be **VERY**
different from **weak-field** gravity



PSR J0348+0333



PSRs J0348+0432 and J1738+0333



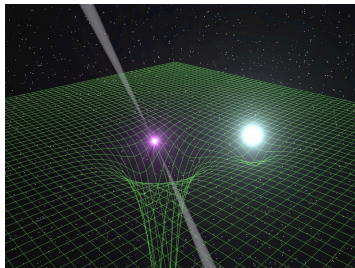
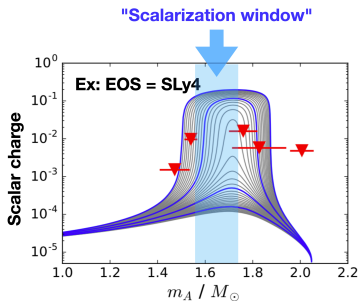
Due to their **asymmetry**, neutron-star white-dwarf systems

provide stringent limits on dipole radiation $\dot{P}_b^{\text{dipole}} \propto (\alpha_{\text{NS}} - \alpha_0)^2$

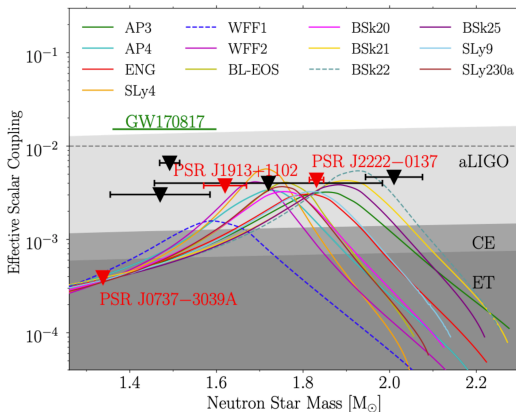
Freire et al. 2012 [arXiv:1205.1450]; Antoniadis et al. 2013 [arXiv:1304.6875]

Combination of Multiple NS-WD Binaries

- Strong-field effects could happen at different NS masses for different EOSs [Shibata et al. 2014 \[arXiv:1310.0627\]](#)
- Combining NS-WDs put the best limits on a class of scalar tensor theories for different EOSs [Shao et al. 2017 \[arXiv:1704.07561\]](#)



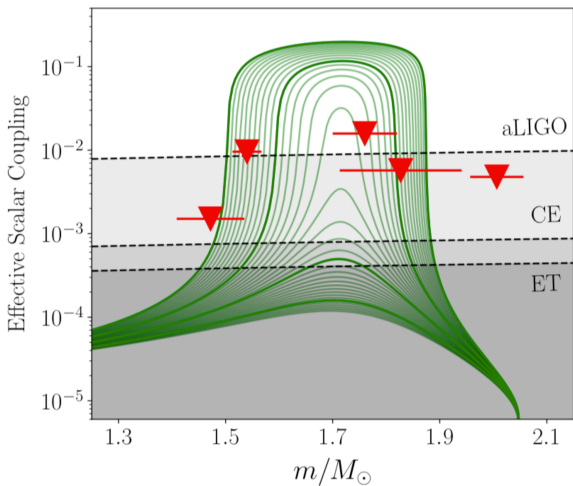
Combination of Multiple NS-WD Binaries



Scalarization window is closed for $T(\varphi_0, \beta_0)$ theories ($\lesssim 1\%$)
with addition of new observations

Zhao et al. 2022 [arXiv:2201.03771]

Gravitational Waves



Will 1994; Damour & Esposito-Farèse 1998; Shao et al. 2017

4. Massive Gravity

Radiative tests are truly powerful
not only in dipole radiation

in other aspects as well

Linearized Fierz-Pauli Theory

- **Linearized gravity** with a massive graviton

$$S = \frac{1}{64\pi} \int d^4x \left[\partial_\lambda h_{\mu\nu} \partial^\lambda h^{\mu\nu} - 2\partial^\nu h_{\mu\nu} \partial_\lambda h^{\mu\lambda} + 2\partial^\nu h_{\mu\nu} \partial^\mu h - \partial^\mu h \partial_\mu h - 32\pi h_{\mu\nu} T^{\mu\nu} + m_g^2 \left(h_{\mu\nu} h^{\mu\nu} - \frac{1}{2} h^2 \right) \right]$$

- The **unique** mass term for $h_{\mu\nu}$ when

- 1 standard form for wave equation

$$(\square - m_g^2) \bar{h}_{\mu\nu} + 16\pi T_{\mu\nu} = 0$$

- 2 recovery of GR when $m_g \rightarrow 0$: no **van Dam-Veltman-Zakharov discontinuity**

Finn & Sutton 2002 [[arXiv:gr-qc/0109049](https://arxiv.org/abs/gr-qc/0109049)]

Linearized Fierz-Pauli Theory

- **Binary pulsars** can be used to constrain the graviton mass via bounding the **gravitational backreaction**

$$\Delta \equiv \frac{L_{\text{GW}} - L_{\text{GW}}^{(\text{GR})}}{L_{\text{GW}}^{(\text{GR})}} \propto m_g^2 \left(\frac{c^2 P_b}{2\pi\hbar} \right)^2$$

- Bayesian analysis with a list of binary pulsars

(collected in Particle Data Group) [Miao, Shao, Ma 2019 \[arXiv:1905.12836\]](#)

PSR	P_b (day)	e	$m_p (M_\odot)$	$m_c (M_\odot)$	$\dot{p}_b^{\text{intr}} (10^{-12})$	Δ
J0348 + 0432 [39]	0.102424062722(7)	0.0000026(9)	2.01(4)	0.172(3)	-0.273(45)	0.05(18)
J0737 - 3039 [40,41]	0.10225156248(5)	0.0877775(9)	1.3381(7)	1.2489(7)	-1.252(17)	0.000(1)
J1012 + 5307 [42,43]	0.60467271355(3)	0.0000012(3)	1.83(11)	0.174(7)	-0.015(15)	0.36(145)
B1534 + 12 [44,45]	0.420737298879(2)	0.27367752(7)	1.3330(2)	1.3455(2)	-0.174(11)	-0.096(57)
J1713 + 0747 [46]	67.8251299228(5)	0.0000749403(7)	1.33(10)	0.290(11)	0.03(15)	-5000(25000)
J1738 + 0333 [47]	0.3547907398724(13)	0.00000034(11)	$1.46_{-0.05}^{+0.06}$	$0.181_{-0.007}^{+0.008}$	-0.0259(32)	-0.072(130)
J1909 - 3744 [48]	1.533449474329(13)	0.00000021(9)	1.540(27)	0.2130(24)	-0.006(15)	2.08(521)
B1913 + 16 [49]	0.322997448918(3)	0.6171340(4)	1.438(1)	1.390(1)	-2.398(4)	-0.0017(16)
J2222 - 0137 [50]	2.44576456(13)	0.000380940(3)	1.84(6)	1.323(25)	-0.063(85)	-1.3(117)

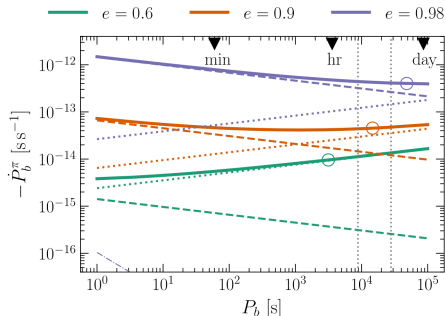
Cubic Galileon

- **Cubic Galileon** with screening mechanics [de Rham et al. 2013]

$$S = \int d^4x \left[-\frac{1}{4} h^{\mu\nu} (\mathcal{E}h)_{\mu\nu} + \frac{h^{\mu\nu} T_{\mu\nu}}{2M_{\text{Pl}}} - \frac{3}{4} (\partial\pi_s)^2 \left(1 + \frac{1}{3\Lambda^3} \square\pi_s \right) + \frac{\pi_s T}{2M_{\text{Pl}}} \right]$$

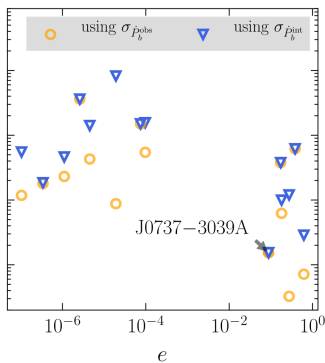
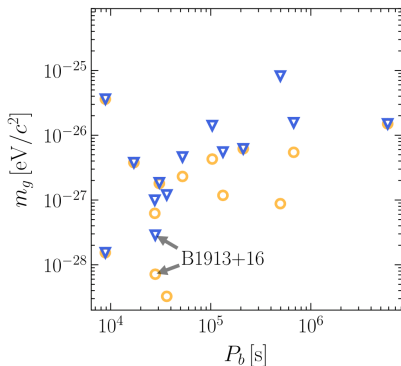
- Extra radiating channels are introduced

- monopole radiation
- dipole radiation
- quadrupole radiation



Shao, Wex, Zhou 2020 [arXiv:2007.04531]

Cubic Galileon



$$m_g \lesssim 2 \times 10^{-28} \text{ eV}/c^2 \quad (95\% \text{ C.L.})$$

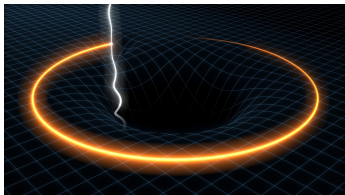
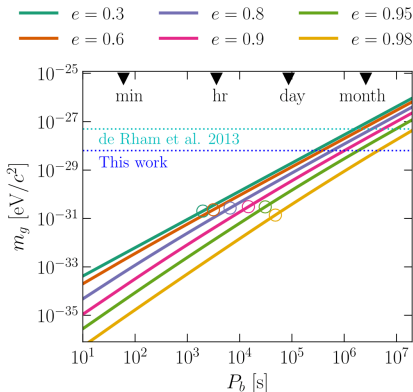
(collected in Particle Data Group)

Shao, Wex, Zhou 2020 [arXiv:2007.04531]

Cubic Galileon

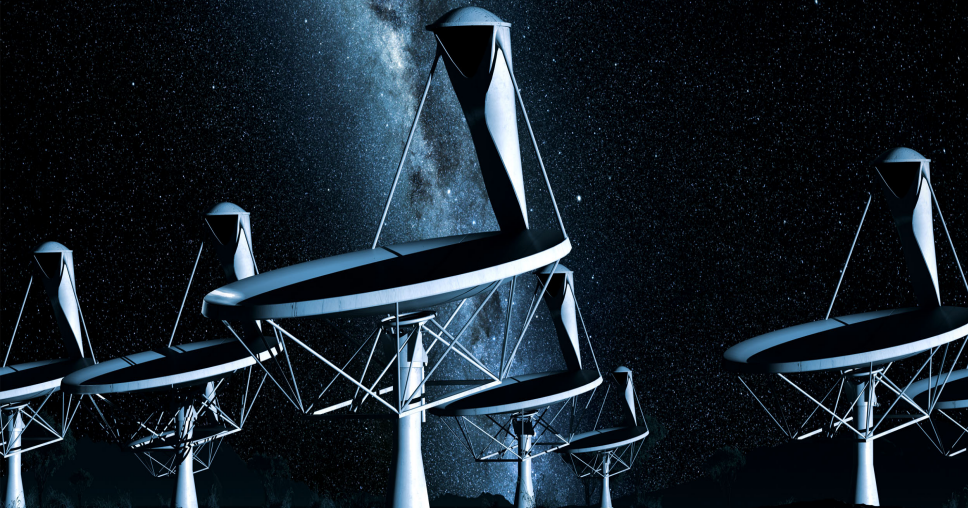
- We also investigated future **pulsar-BH** and **pulsar-Sgr A*** systems, in constraining the mass of graviton

- MeerKAT, FAST, SKA, etc

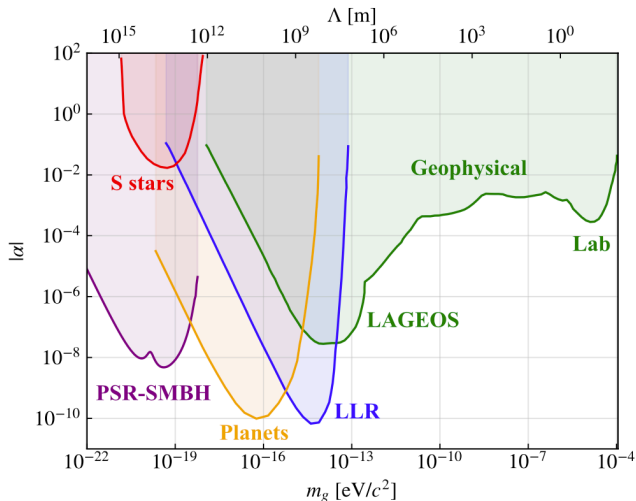


Shao, Wex, Zhou 2020 [arXiv:2007.04531]

Square Kilometre Array



Yukawa Gravity: Pulsars around Sgr A*



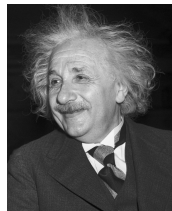
Dong, Shao, et al. 2022, JCAP [arXiv:2210.16130]

5. Fifth Force from Dark Matters

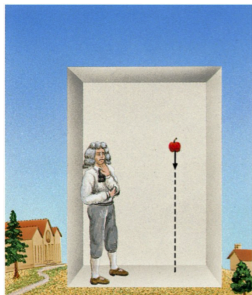
Conservative dynamics are also
good friends

...in many aspects

Equivalence Principle

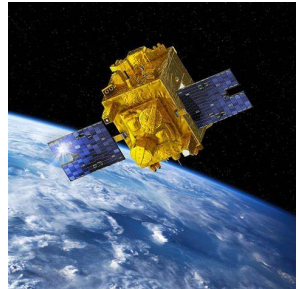
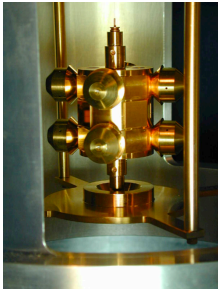


- Einstein's **General Relativity** (1915)
 - 1 Galilei's Relativity Principle
 - 2 Equivalence Principle (**EP**)
- **EP**: *Locally*, **gravity = accelerated system**



Tests of Equivalence Principle

- Galilei, Newton, Bessel, Potter
- Eötvös, Dicke, Braginsky, Adelberger $\sim 10^{-13}$
- Lunar laser ranging $\sim 10^{-13}$
- MICROSCOPE satellite $\sim 10^{-15}$



Strong Equivalence Principle

- How about “gravitational energy”? Nonlinearities?
- **Strong EP**: self-gravitating bodies also have $m_i = m_g$

$$\epsilon \sim \frac{GM}{Rc^2} \sim \left\{ \begin{array}{ll} 10^{-10}, & \text{Moon} \\ 10^{-9}, & \text{Earth} \\ 10^{-6}, & \text{Sun} \\ 0.2, & \text{Neutron Stars} \end{array} \right.$$

- GR is the **only** valid theory that preserves SEP

Will 2014; Adelberger et al. 2009; Shao & Wex 2016, SCPMA 59:699501

Damour-Schäfer Test

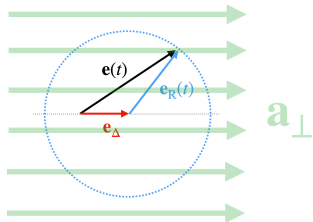
- For a binary pulsar in the Galactic potential (acceleration $\mathbf{a} \sim 2 \times 10^{-10} \text{ m s}^{-2}$), there is an extra acceleration from **SEP violation**

$$\mathbf{a}_{\Delta} = (\Delta_p - \Delta_c) \mathbf{a}$$

- At the 1 PN approximation, when the E.o.M.s is integrated, the evolution of **eccentricity vector** is

[Damour & Schäfer 1991, PRL 66:2549]

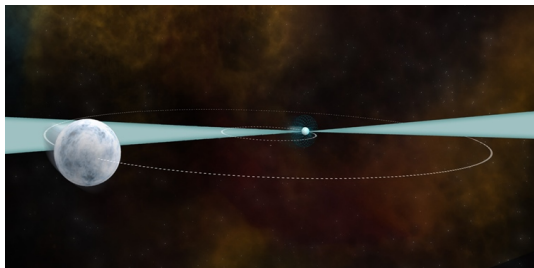
$$\mathbf{e}(t) \equiv e\hat{\mathbf{a}} = \mathbf{e}_{\text{PN}}(t) + \mathbf{e}_{\Delta}$$



Shao 2023 [arXiv:2206.15187]

Damour-Schäfer Test

- Combined timing analysis on PSR J1713+0747 from NanoGRAV and EPTA [Zhu *et al.* 2019, MNRAS 482:3249]
 - $P_b = 67.8$ d, $e = 0.00007$
 - $m_p = 1.33 M_\odot$ (neutron star), $m_c = 0.29 M_\odot$ (white dwarf)
- Constraint on the **universality of free fall**: $\Delta \lesssim 0.002$



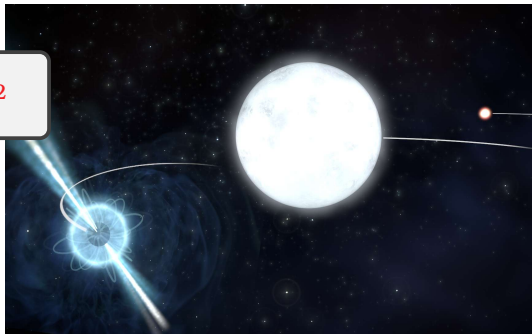
Triple Pulsar

- A millisecond pulsar in a stellar triple system

[Ransom *et al.* 2014, *Nature* 505:520; Archibald *et al.* 2018, *Nature* 559:73]

- $P_{b,I} = 1.6 \text{ d}$, $e_I = 0.0007$; $P_{b,O} = 327 \text{ d}$, $e_O = 0.04$
- $m_p = 1.44 M_\odot$ (neutron star), $m_{c,I} = 0.20 M_\odot$ & $m_{c,O} = 0.41 M_\odot$
(white dwarfs)

$$a \sim 2 \times 10^{-3} \text{ m s}^{-2}$$



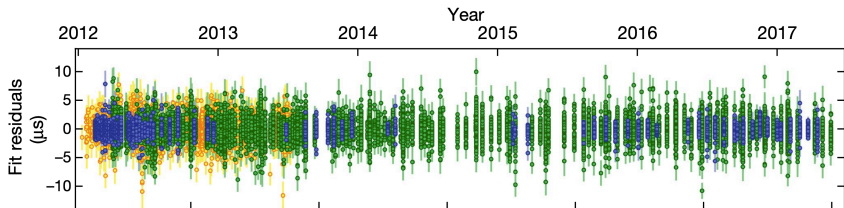
Freire *et al.* 2012, *CQG* 29:184007

Shao 2016, *PRD* 93:084023

Triple Pulsar and the SEP

- The **universality of free fall** was constrained to

$$\Delta \begin{cases} \lesssim 2.6 \times 10^{-6}, & [\text{Archibald et al. 2018, Nature 559:73}] \\ = (0.5 \pm 1.8) \times 10^{-6}, & [\text{Voisin et al. 2020, A\&A 638:A24}] \end{cases}$$

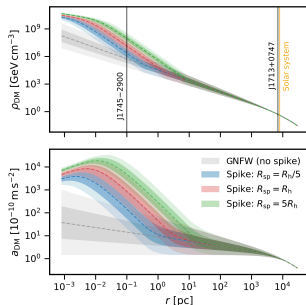
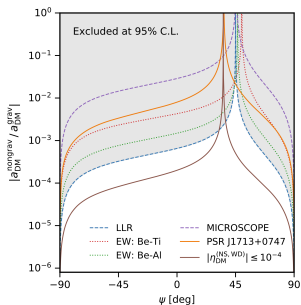


SEP and Dark Matter

- The “third” body in the [Damour-Schäfer test](#) is our Milky Way, which has a significant composition of **dark matters**
- We propose a novel SEP-like test to constrain the **fifth force** from dark matters [Shao et al. 2018, PRL \[arXiv:1805.08408\]](#)
 - 1 Large **material difference** in test-body pairs (**NS vs WD**)
 - 2 Significant **gravitational binding energy**
- **Binary pulsar** PSR J1713+0747 gives the best constraint, while the **triple pulsar** does not apply here
 - No dark matters involved in the triple pulsar system

SEP and Dark Matter

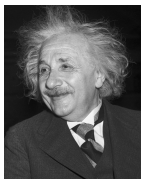
- If there is a long-range **fifth force**, it should be smaller than $1\% \times \text{gravity} \Leftarrow$ PSR J1713+0747 Shao et al. 2018 [arXiv:1805.08408]
- Because of the dark matter spike, binary pulsars within about 10 pc from the **Galactic center** will be extremely helpful in future



6. Summary

Summary

- Radio pulsars are **precision** clocks
 - Sensitive to tiny deviation from GR in dynamics
- Extremely useful in **fundamental physics**
 - spacetime symmetries
 - strong-field gravity theories
 - massive gravity
 - strong equivalence principle
 - dark matters
 - ...
- **Einstein is *still* right**



Thank you!

